

# The $\pi^0$ Lifetime: Experimental Probe of the QCD Axial Anomaly

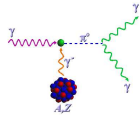
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## The $\pi^0$ Lifetime: Experimental Probe of the QCD Axial Anomaly

### Outline

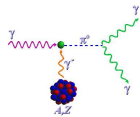
- Physics Motivation
- Experimental Overview
- Calibration Reactions
  - Pair Production
  - Compton Scattering
- $\pi^0$  Analysis Details
- Preliminary  $\Gamma_{\pi^0 \rightarrow \gamma\gamma}$  Result
- Summary and Outlook



## PrimEx Collaboration

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(m) University of North Carolina, Wilmington, (n) Northwestern University,  
(o) Institute for High Energy Physics, Protvino, (p) University of Sao Paulo,  
(q) University of Virginia, (r) Virginia Tech, (s) Yerevan Physics Institute

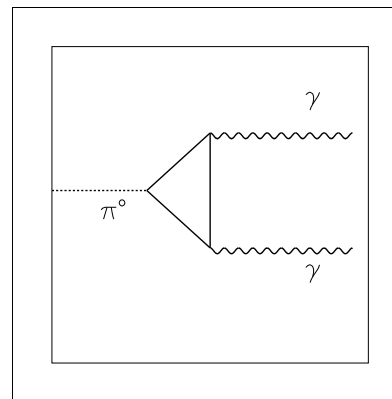


## Physics Motivation

- $\pi^0$  decay rate is a fundamental prediction of QCD.

### Chiral Anomaly

Presence of closed loop triangle diagram results in nonconserved axial vector current, even in the limit of vanishing quark masses.

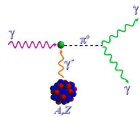


→ In the leading order (chiral limit), the anomaly leads to the decay width:

$$\Gamma_{\pi^0 \rightarrow \gamma\gamma} = \frac{\alpha^2 m_\pi^3}{64\pi^3 F_\pi^2} = 7.725 \pm 0.044 \text{ eV} \quad (1)$$

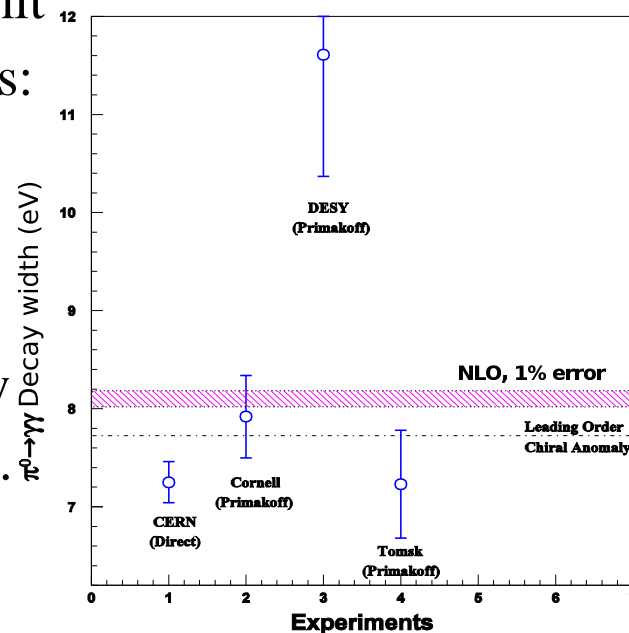
where  $F_\pi = 92.42 \pm 0.25 \text{ MeV}$  is the pion decay constant.

→ Current Particle Data Book value is  $7.84 \pm 0.56 \text{ eV}$



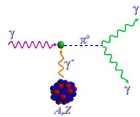
## Physics Motivation

- LO prediction exact in Chiral limit
- For  $m_q \rightarrow 0$ , there are corrections:
  - Due to isospin sym-breaking ( $m_u \neq m_d$ ),  $\pi^0$ ,  $\eta$  and  $\eta'$  mixing induced.
  - Further corrections induced by terms in the Chiral Lagrangian.
- NLO prediction for the decay width is  $8.10 \text{ eV} \pm 1\%$ 
  - Calc. using Chiral Perturbation Theory and  $1/N_c$  expansion.
- A precision measurement of the  $\pi^0$  decay width is needed.



J.L.Goity et al, Phys. Rev. D66, 076014 (2002); B.Moussallam, Phys. Rev. D51, 4939 (1995)

→ This is 4% higher than current experimental value!



## CERN (Direct Method) Decay Length Measurement

→  $\tau_{\pi^0} \sim 1 \times 10^{-16}$  s  $\Rightarrow$  too small to measure

→ Solution—Measure decay length of highly energetic  $\pi^0$ 's:

$$L = v\tau_{\pi^0}E/m \quad (2)$$

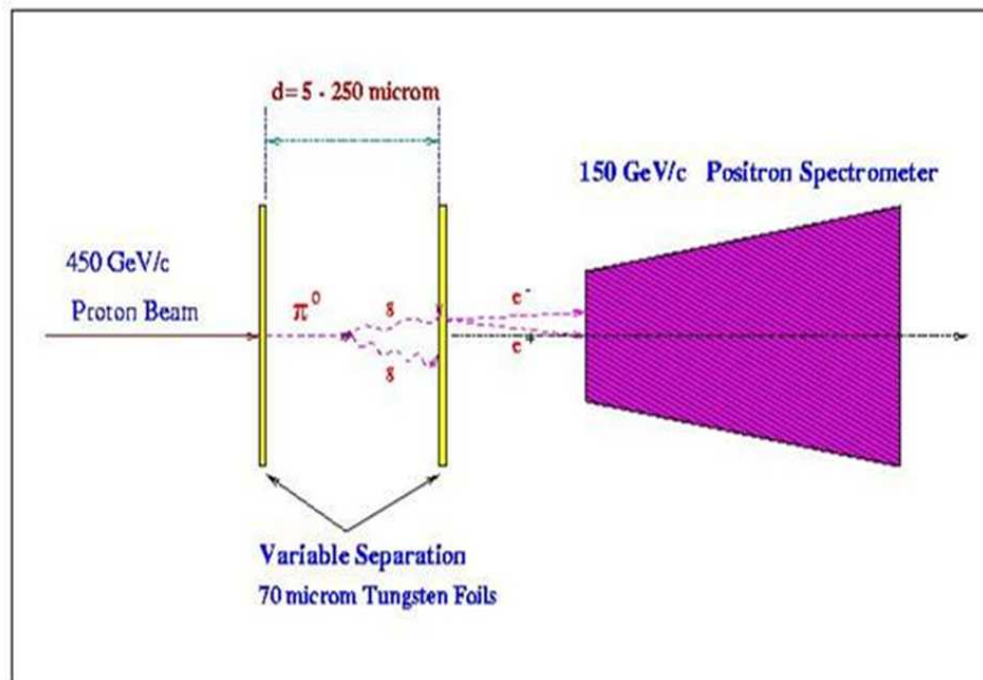
→ for  $E = 1000\text{GeV}$ ,  $L \sim 100\mu\text{m}$  (very challenging experiment)

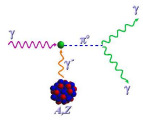
→ Performed in 1984:  
Used 450GeV protons

→ Result:

$$\Gamma_{(\pi^0 \rightarrow \gamma\gamma)} = 7.34\text{eV} \pm 3.1\%$$

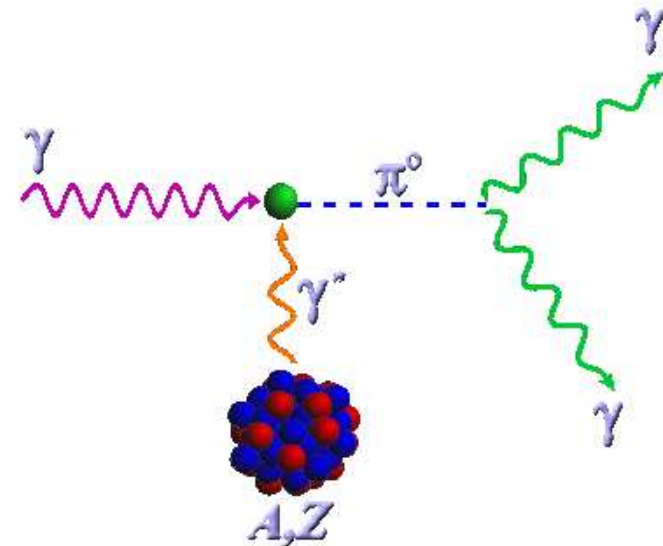
→ Dominant syst. error:  
Uncertainty in  $E_{\pi^0}$  ( $\pm 1.5\%$ )



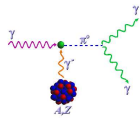


## The Primakoff Effect

- $\pi^0$  photoproduction from Coulomb field of nucleus.
- Equivalent production ( $\gamma\gamma^* \rightarrow \pi^0$ ) and decay ( $\pi^0 \rightarrow \gamma\gamma$ ) mechanism implies Primakoff cross section proportional to  $\pi^0$  lifetime.
- Primakoff  $\pi^0$  produced at very forward angles.



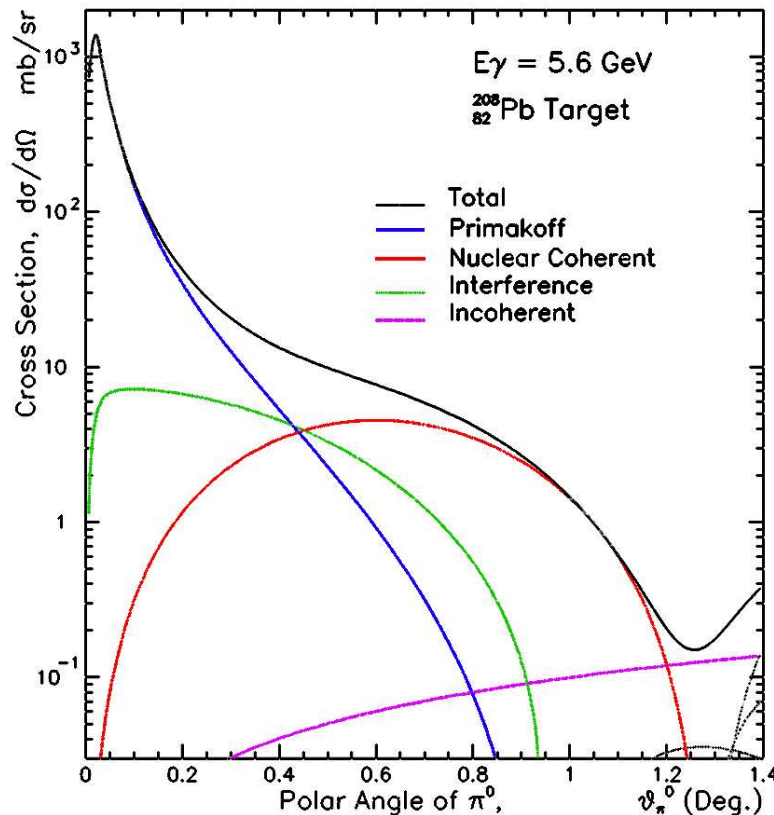
$$\frac{d\sigma_P}{d\Omega} = \Gamma_{(\pi^0 \rightarrow \gamma\gamma)} \frac{8\alpha_{em} Z^2 \beta^3 E^4}{m^3 Q^4} |\tilde{F}_{em}(Q)|^2 \sin^2 \theta_\pi \quad (3)$$



## Full Cross Section Components

$$\frac{d\sigma_{\pi^0}}{d\Omega} = \frac{d\sigma_P}{d\Omega} + \frac{d\sigma_C}{d\Omega} + \frac{d\sigma_I}{d\Omega} + 2 \cdot \sqrt{\frac{d\sigma_P}{d\Omega} \cdot \frac{d\sigma_C}{d\Omega}} \cos(\phi) \quad (4)$$

Primakoff    Nucl.Coherent    Incoherent    Interference



**Primakoff:**

Proportional to  $Z^2$ ,  
peaked at  $\theta_{\pi^0} = m_{\pi^0}^2 / 2E_\gamma^2$

**Nuclear Coherent:**

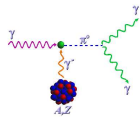
$$\frac{d\sigma_C}{d\Omega} = C \cdot A^2 |F_N(Q)|^2 \sin^2 \theta_\pi \quad (5)$$

**Nuclear Incoherent:**

$$\frac{d\sigma_I}{d\Omega} = \xi A (1 - G(Q)) \frac{d\sigma_H}{d\Omega} \quad (6)$$

**Interference:**

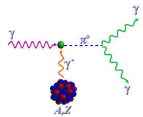




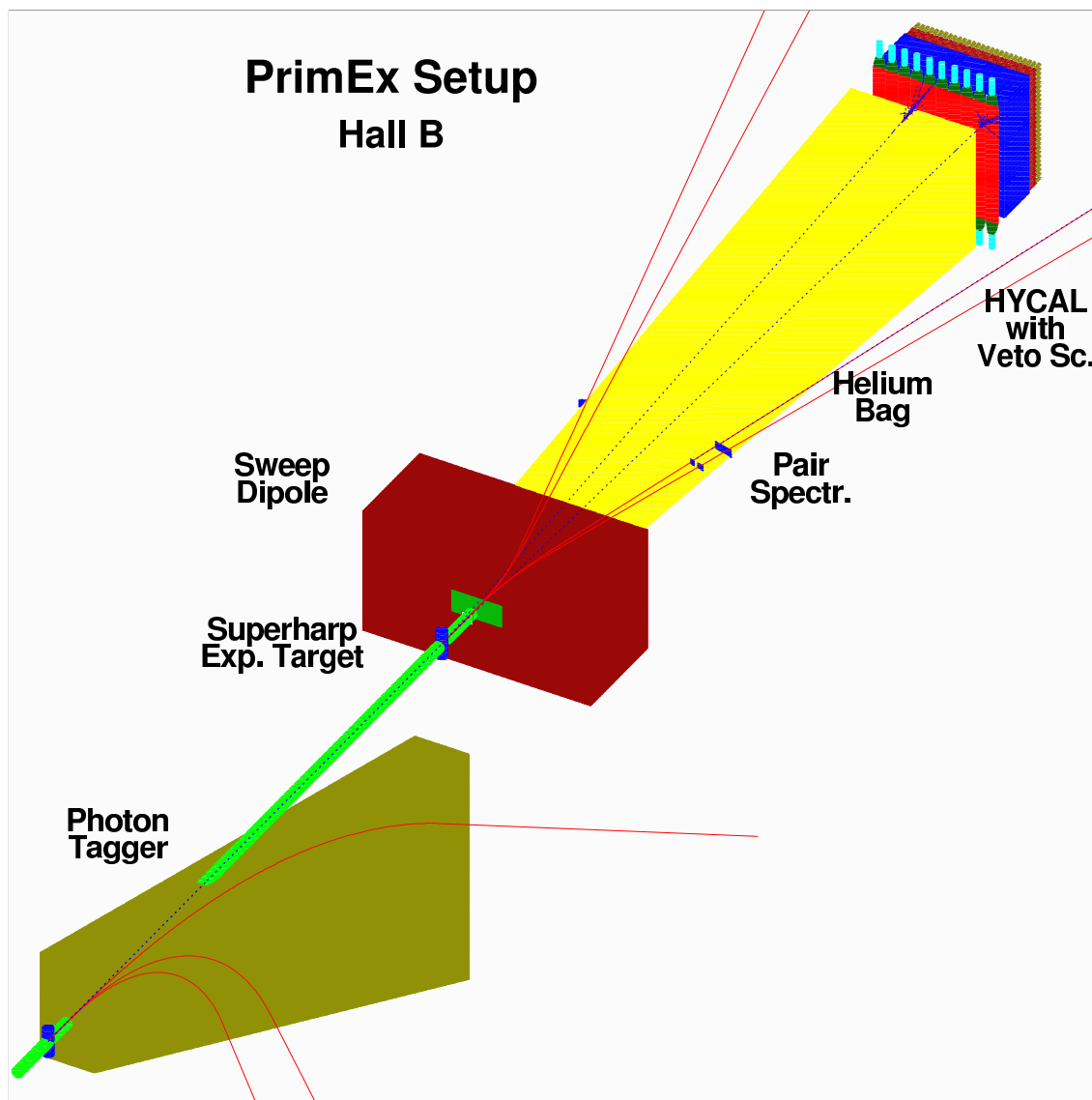
## Experiment Overview

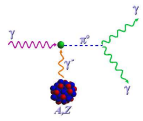


- Conducted at Jefferson Lab, Fall 2004
  - Used 5.75 GeV continuous  $e^-$  beam and Hall B  $\gamma$ -tagging facility
  - Tagged photons incident on 5%  $X_0$  targets:  $^{12}\text{C}$  and  $^{208}\text{Pb}$
  - New PrimEx/Hall B calorimeter (HyCal), upstream of CLAS, designed to detect  $\pi^0$  decay  $\gamma$ 's
- 
- Measured 3 physical processes (absolute cross sections): Primary -  $\pi^0$  production, Secondary - Compton and  $e^+e^-$  pair production
  - Improvements over previous experiments: Precision tagged  $\gamma$  flux and incident  $\gamma$  energy info, enhanced  $\pi^0$  angular and mass resolution, and identification and subtraction of background event contamination



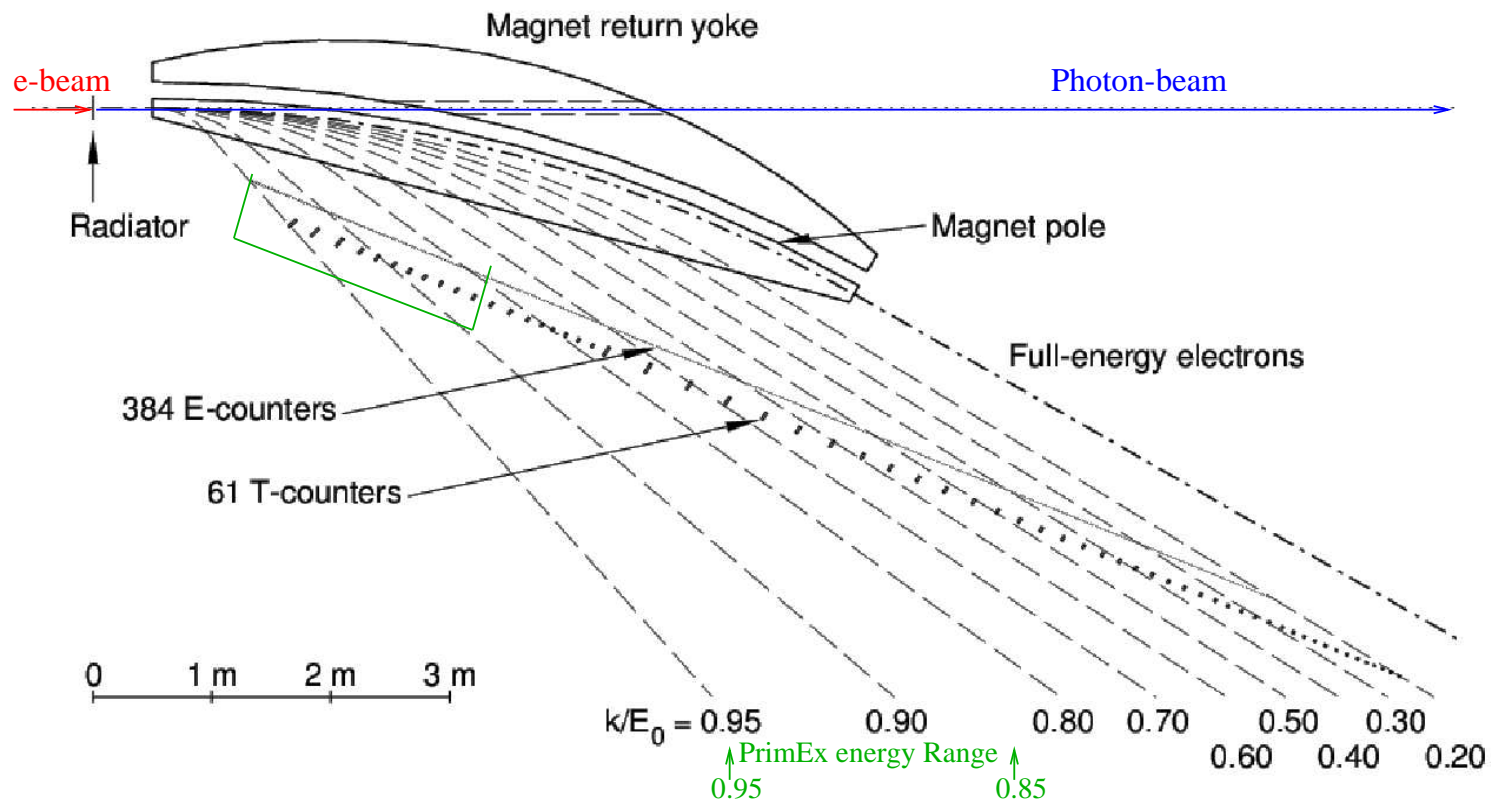
## Experiment Overview

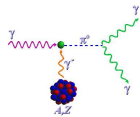




### Hall B Photon Tagger

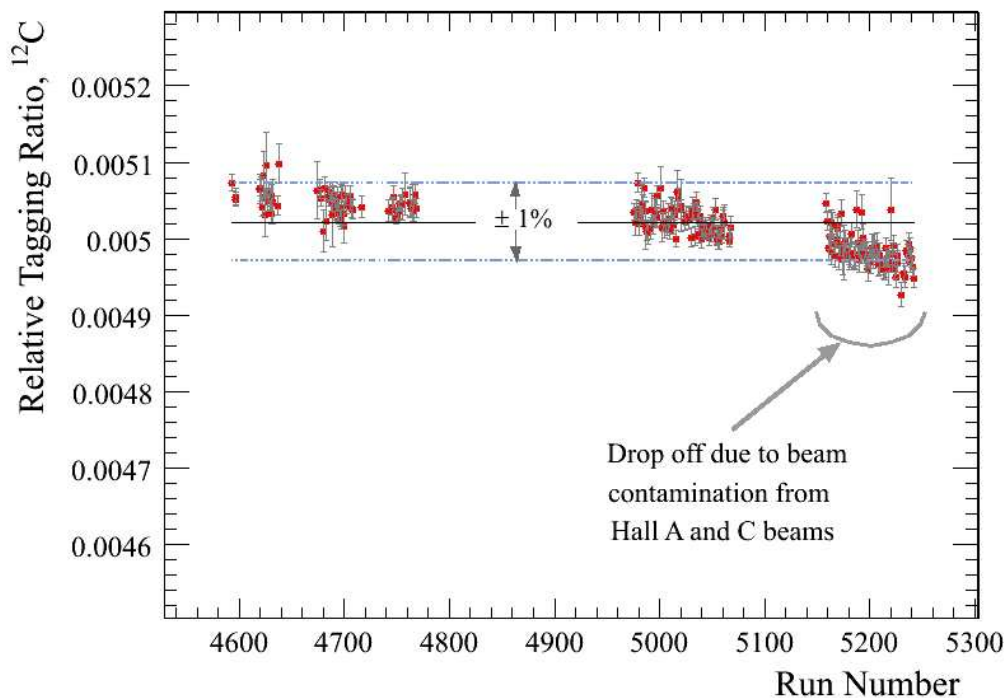
- Single dipole magnet combined with a hodoscope containing two planar arrays of plastic scintillators to detect energy-degraded electrons from a thin bremsstrahlung radiator.
- Tagger has 0.1% energy resolution and is capable of 50 MHz rates.

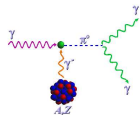




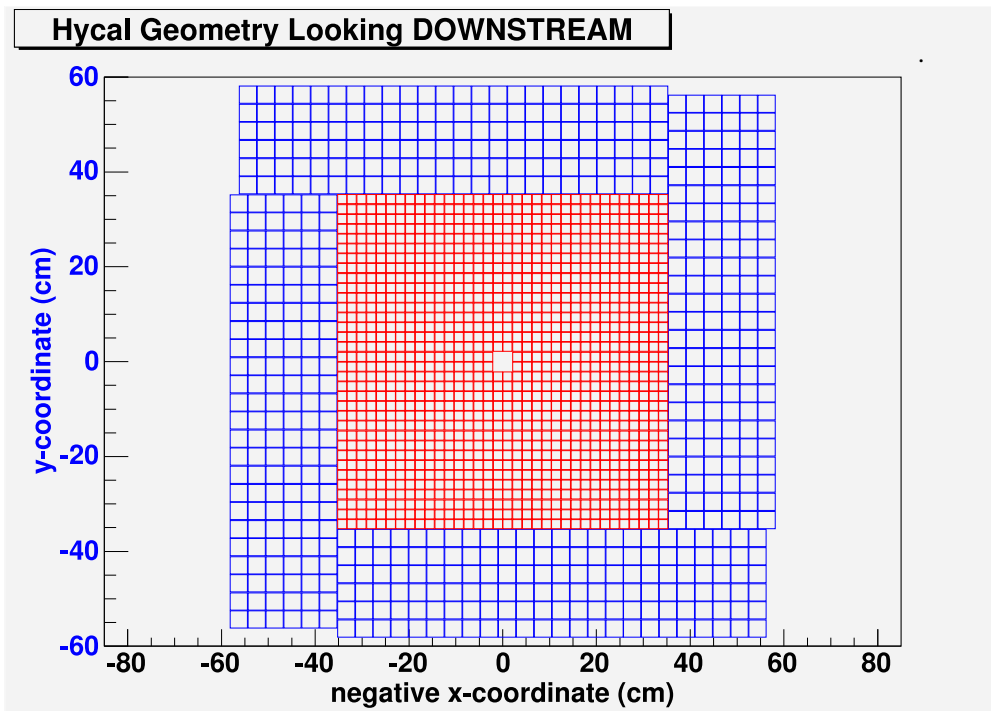
## Photon Flux Control

- PrimEx achievement: Total uncertainty in photon flux = 1.1%.
- Number of tagged photons on target ( $N_\gamma$ ) calibrated periodically using a Total Absorption Counter (TAC).
- Any drifts in the tagging ratio, occurring between calibration points, are monitored online with the  $e^+e^-$  pair spectrometer.



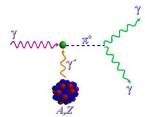


## PrimEx Hybrid Calorimeter – “HyCal”

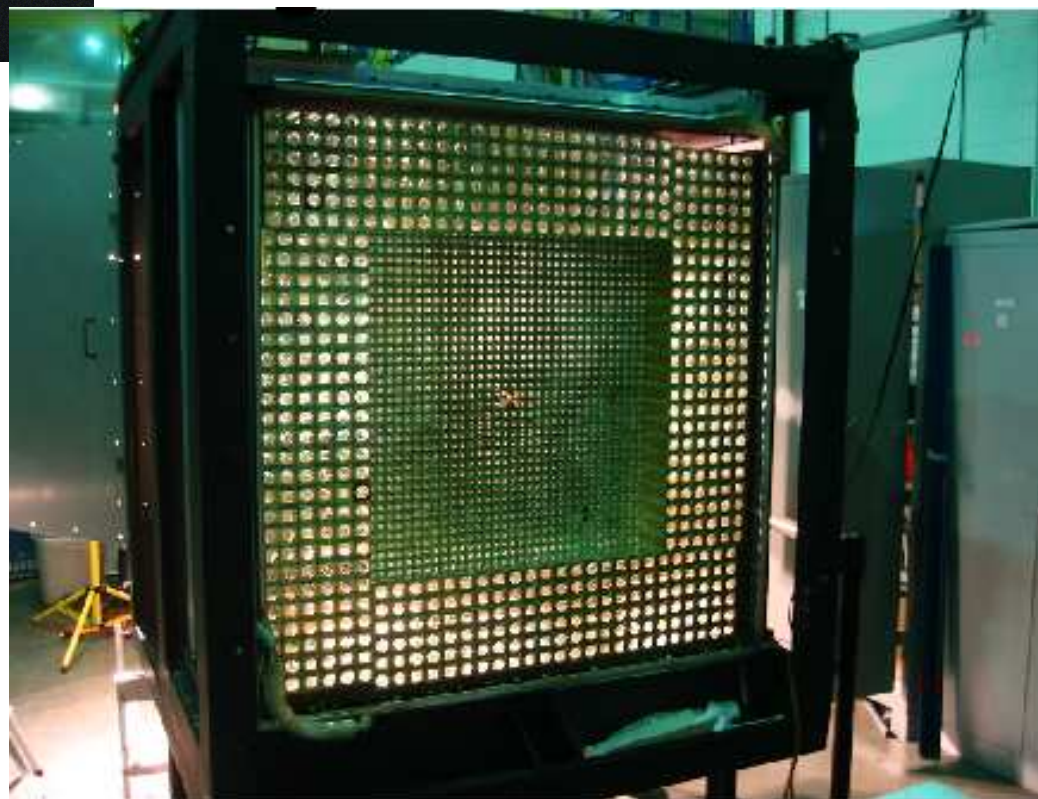
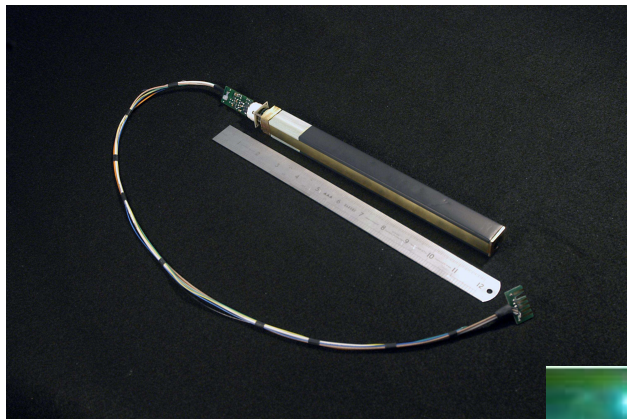


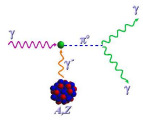
- Optimal performance/cost design
- 1.2 m × 1.2 m, 1728 channels
- 576 Lead-glass (**outer layers**)
- 1152 Lead-Tungstenate crystal (**inner layers**)

	Lead-glass	PbWO <sub>4</sub>
Energy Res. ( $\Delta E/E$ )	3 – 5 %	1 – 2 %
Position Res. ( $\Delta x, y$ )	~ 5 mm	~ 1.5 mm
Angular Res. ( $\Delta\theta_{\pi^0}$ )	~ 675 $\mu\text{rad}$	~ 300 $\mu\text{rad}$



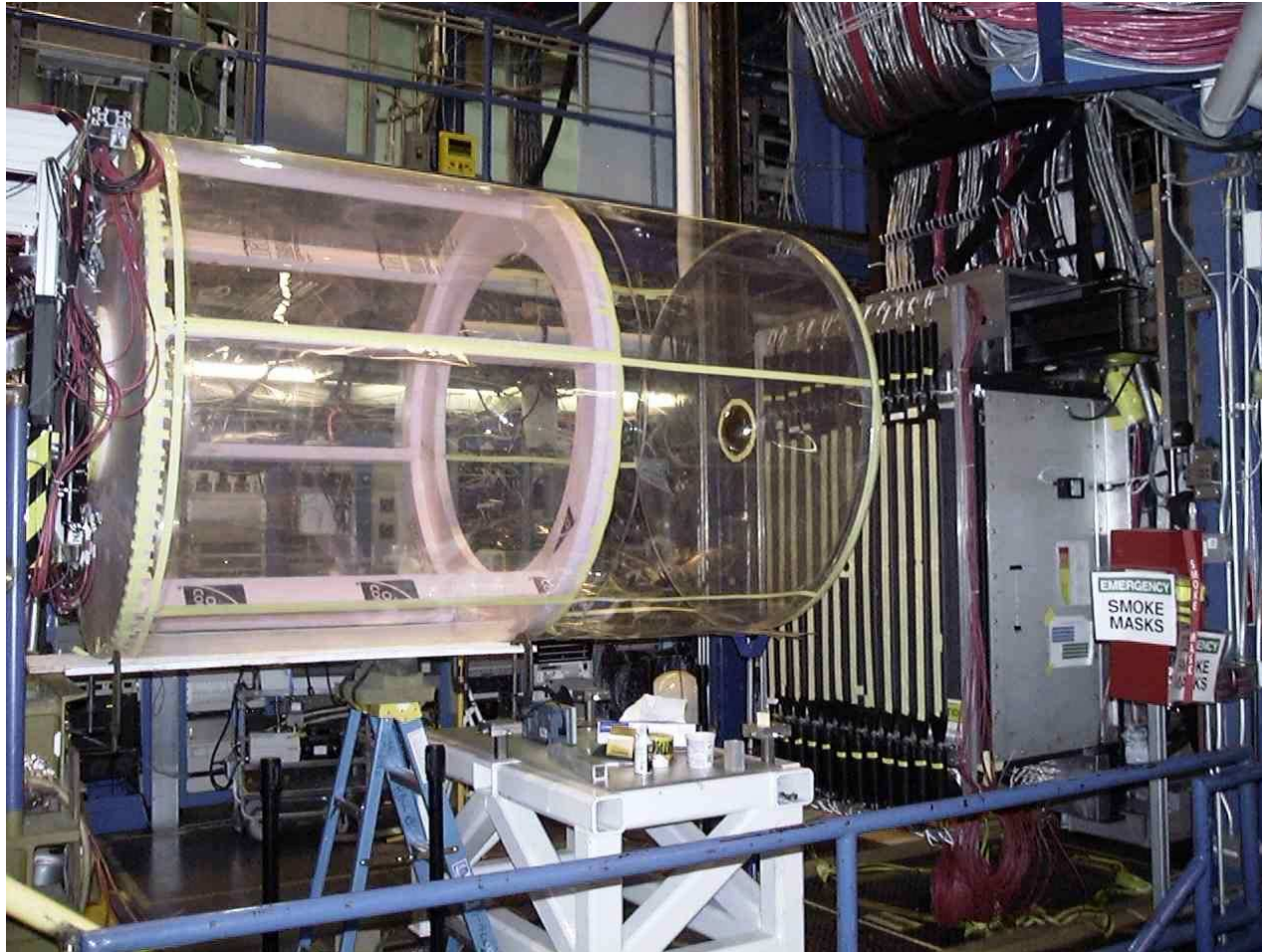
## PrimEx Hybrid Calorimeter – “HyCal”

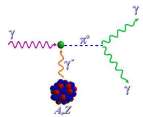




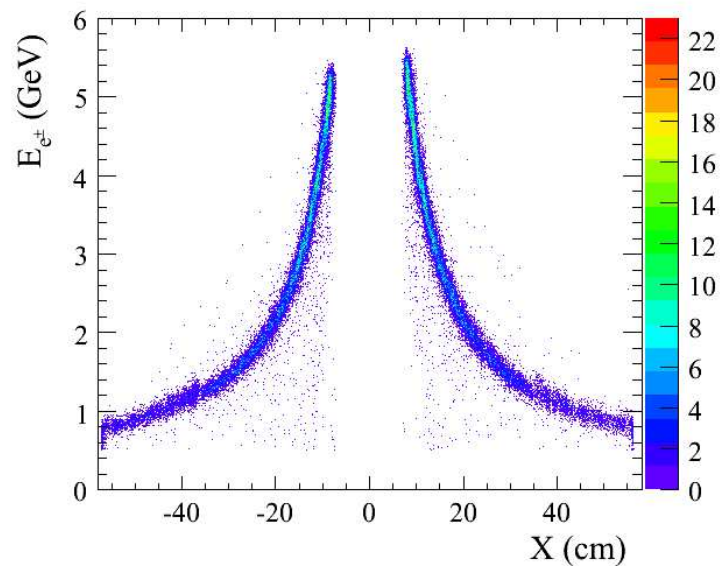
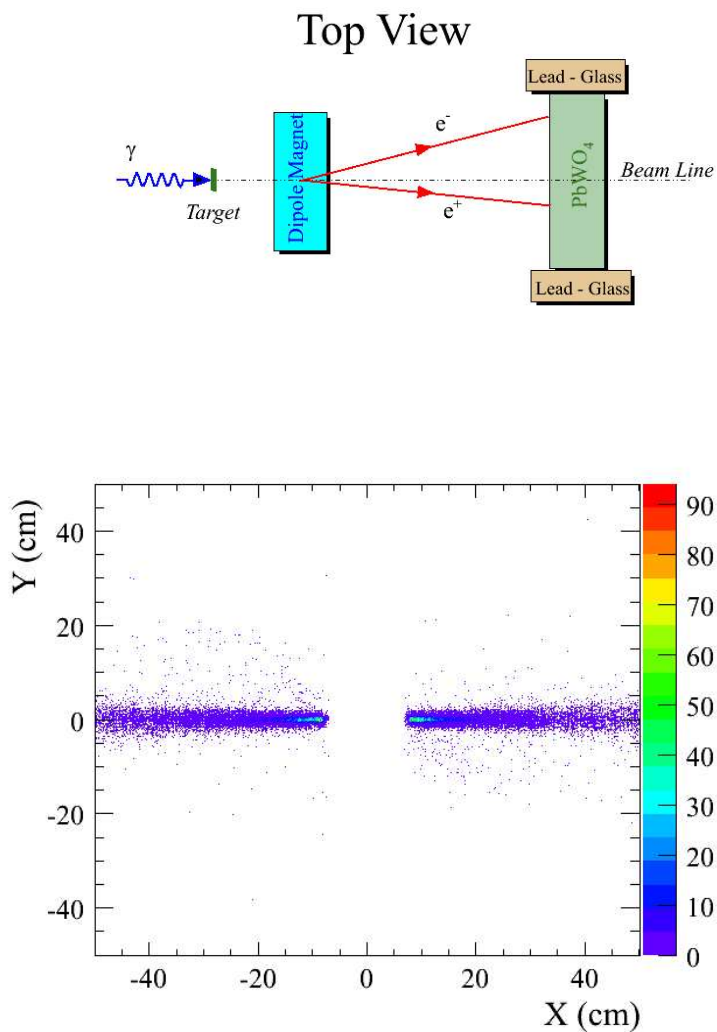
## HyCal Calibration

- Full x,y motion allowed each ch. to be scanned through tagged  $\gamma$  beam.
- Performed at both the beginning and end of the experiment.

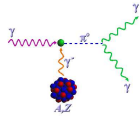




## Calibration Reactions: $e^+ e^-$ Pair Production

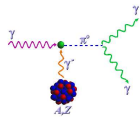




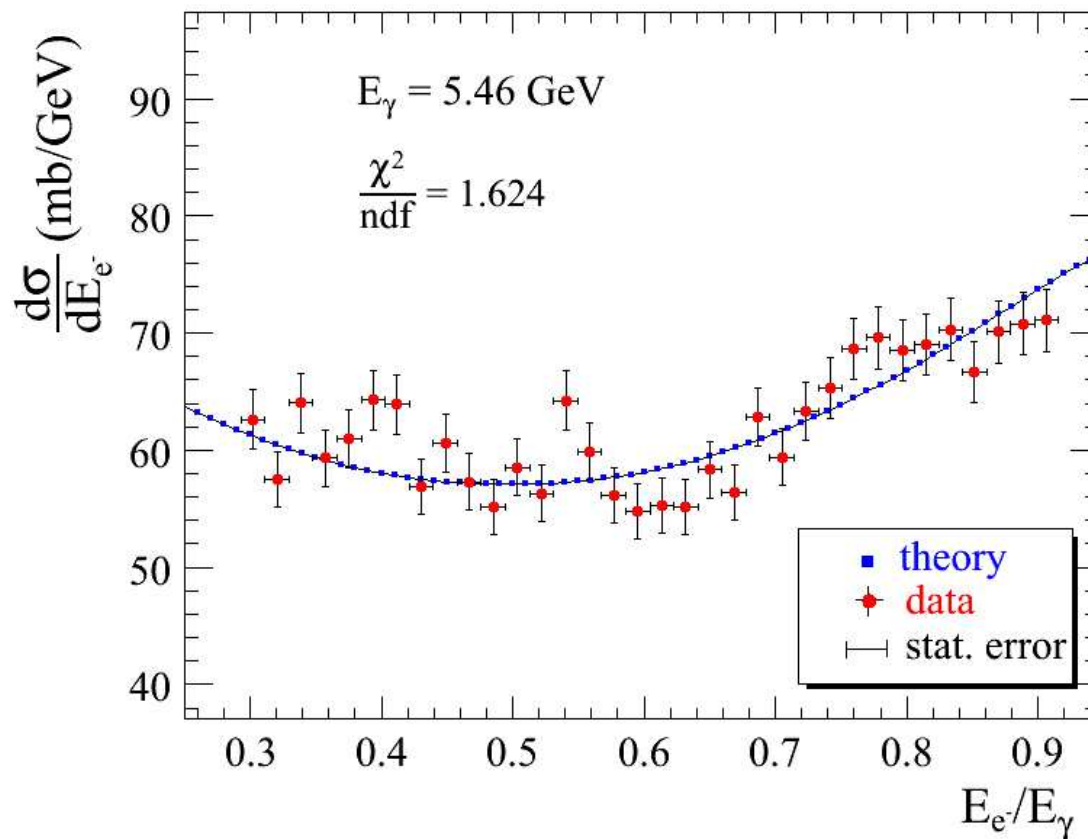


## Calculation of Pair Production Cross Section at PrimEx Kinematics

- Bethe-Heitler mechanism of pair production on the nucleus with screening effects due to atomic electrons and Coulomb distortion
- Pair production off atomic electrons, considering excitation of all atomic states and correlation effects due to the presence of other electrons and the nucleus
- Radiative corrections (of order  $\alpha/\pi$ ) (i) virtual photon loops and (ii) real photon process like  $\gamma + A \rightarrow e^+ + e^- + A + \gamma$
- Nuclear incoherent contribution,  $\gamma + p \rightarrow e^+ + e^- + p$
- Nuclear coherent contribution (VCS),  $\gamma + A \rightarrow \gamma^* + A \rightarrow e^+ + e^- + A$



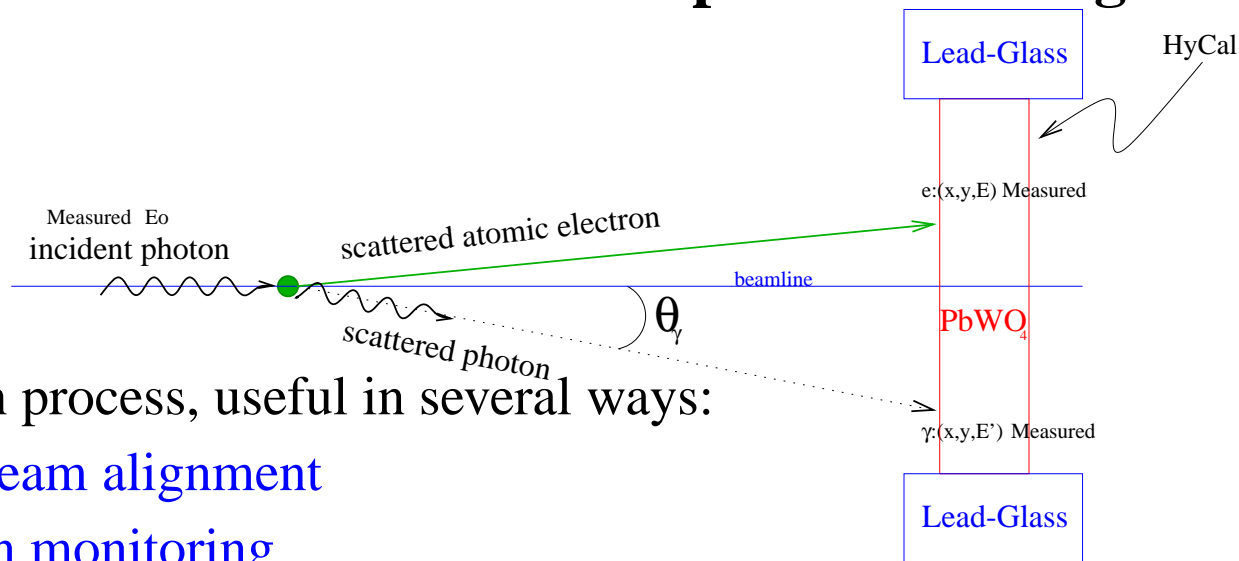
## Pair Production Preliminary Result



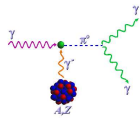
- Agreement with theory at  $\sim 2.5\%$  level
- Work in progress to reduce systematic errors to 1 – 2% level



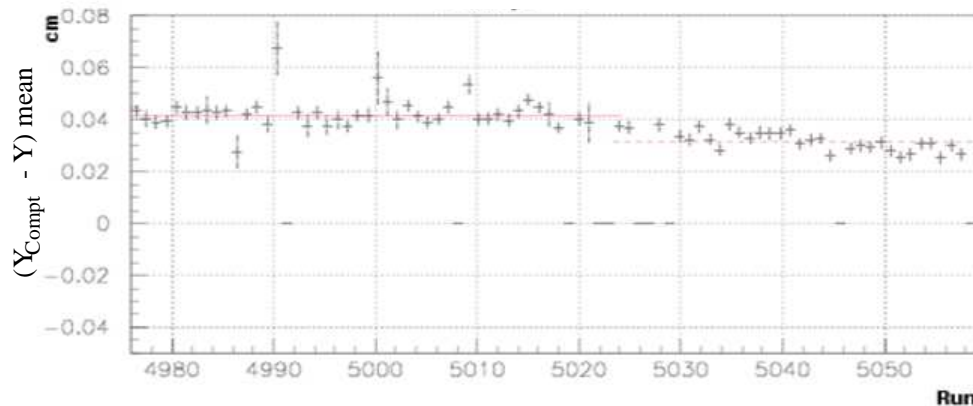
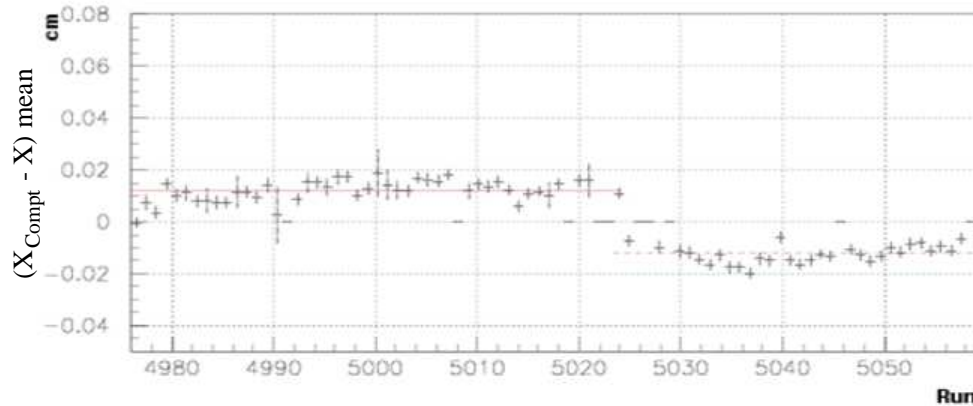
## Calibration Reactions: Compton Scattering



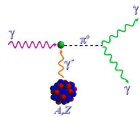
- A well known process, useful in several ways:
  - Detector/beam alignment
  - HyCal gain monitoring
  - Overall check of PrimEx setup to measure absolute cross sections
    - Dedicated "Double-Arm" Compton Runs:
      - Performed on a weekly basis,  $B_{PS} = 0$ ,  $I_{beam} \sim 5 - 10$  nA
      - Both  $e^-$  and scattered photon detected in HyCal
      - Compton Cross Section Measured:  $^{12}C$  and 0.5%  $X_0$   $^4Be$
    - "Single-Arm" Compton Data:
      - Dominant Source of Events in  $\pi^0$  production dataruns
      - $B_{PS} \sim 2$  T,  $I_{beam} \sim 100$  nA, only scattered photon detected



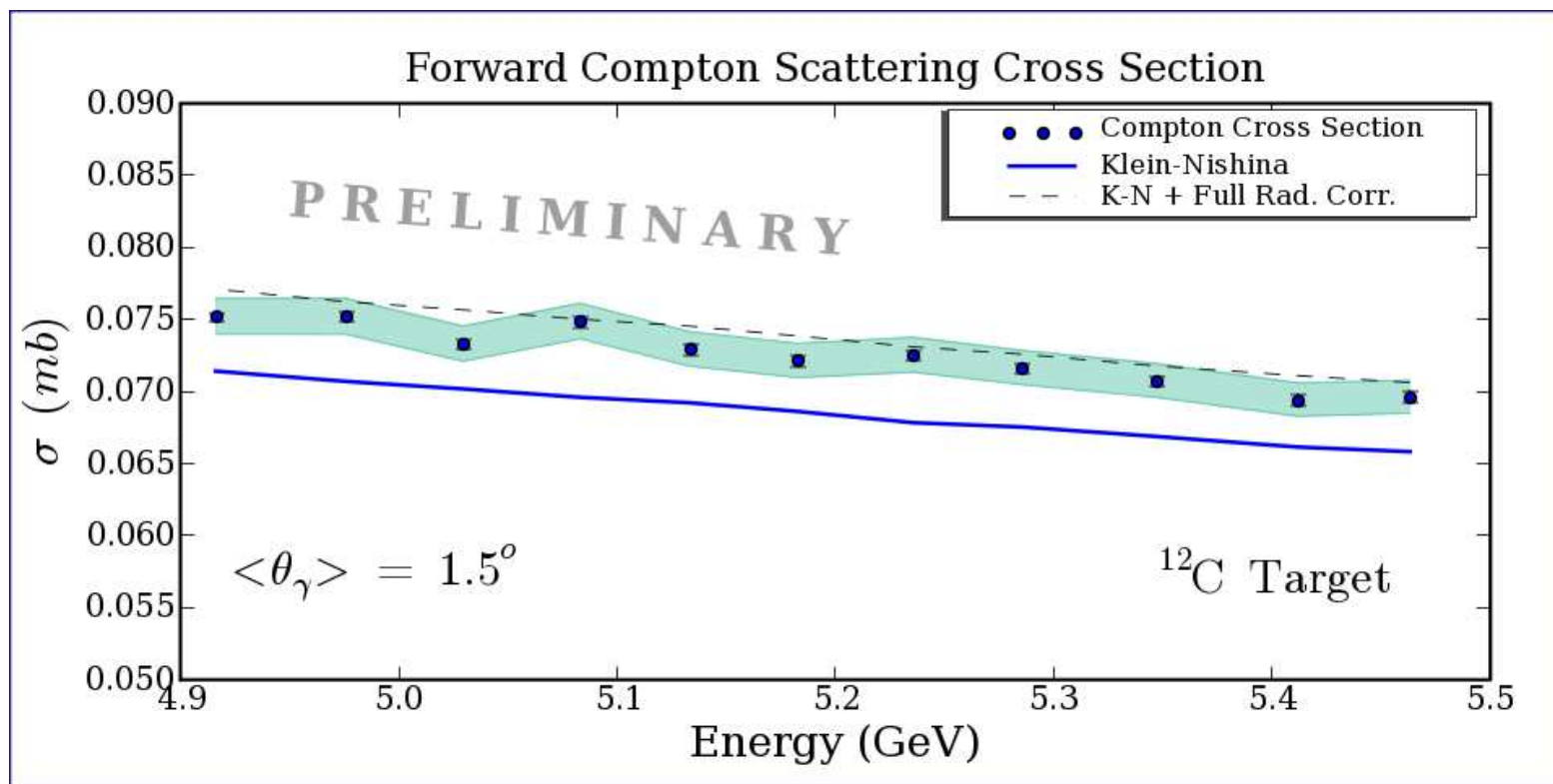
## Beam Alignment Monitoring using Single-Arm Compton



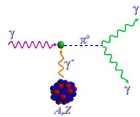
- Only scattered  $\gamma$  measured
- $X \equiv$  reported HyCal coord
- $X_{\text{Compt}} \equiv$  calc. (x,y) from Hycal E and Compton kin.
- If beam alignment perfect:  $(X_{\text{Compt}} - X) = 0$
- Technique tracks alignment at 0.1 mm level
- Jump in X correlated with beamline BPM



## Compton Cross Section Preliminary Result



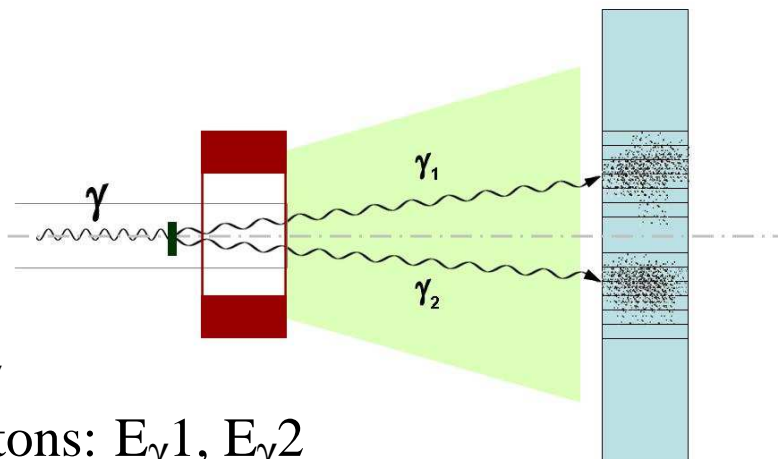
- Total estimated error: 2.5% (dominated by photon flux 1.5%)
- Work in progress to reduce systematic errors to 2% level



## Analysis Details: $\pi^0$ Event Selection

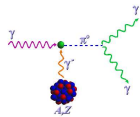
We measure:

- initial photon energy:  $E_\gamma$
- energies of decayed photons:  $E_{\gamma 1}$ ,  $E_{\gamma 2}$
- X, Y positions of decayed photons

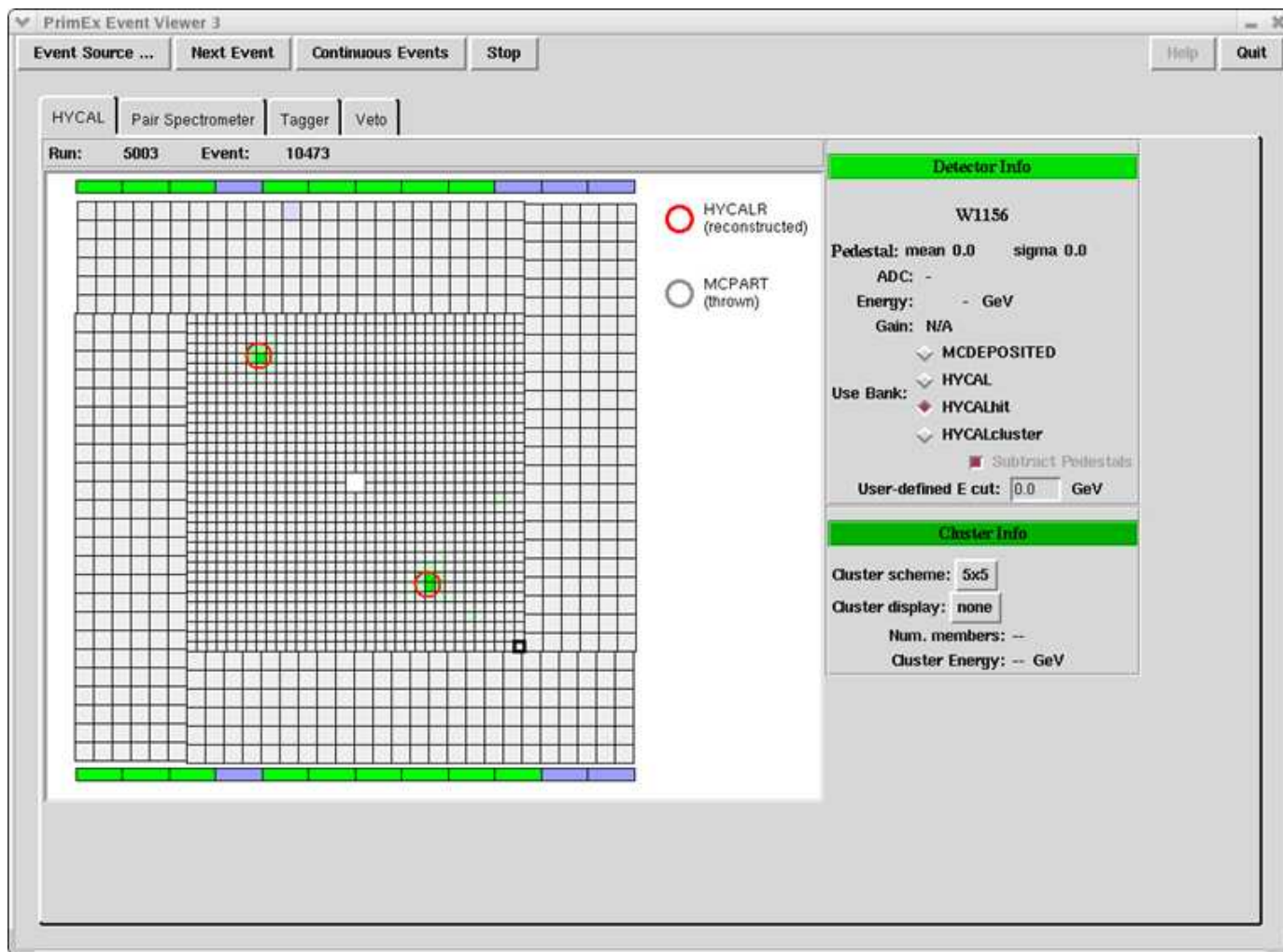


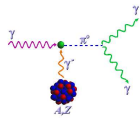
Kinematical constrains:

- Conservation of energy
- Conservation of momentum
- $m_{\gamma\gamma}$  invariant mass



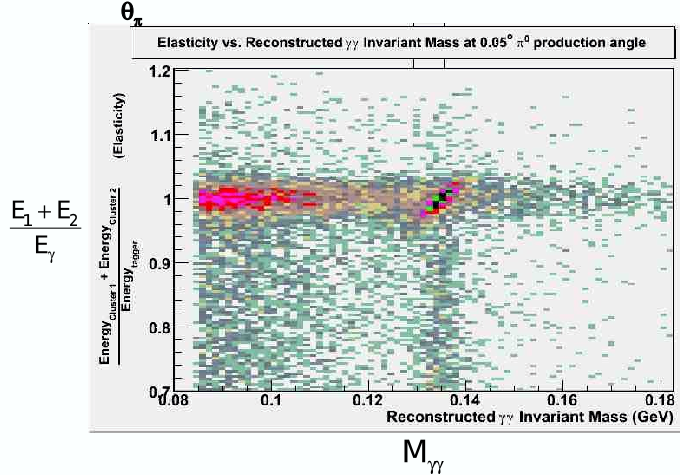
## Analysis Details: $\pi^0$ Event Selection



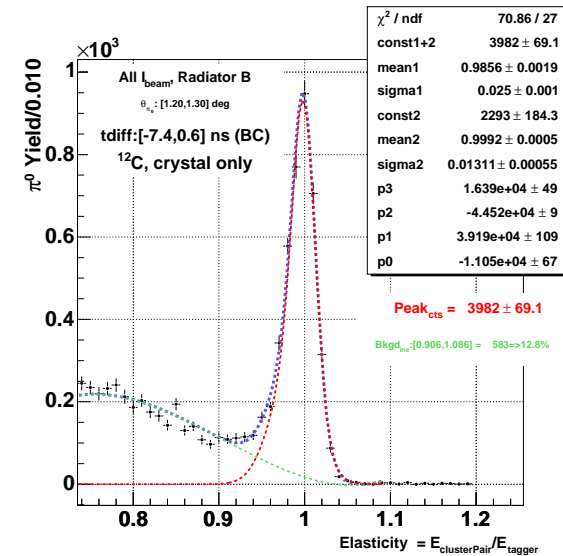
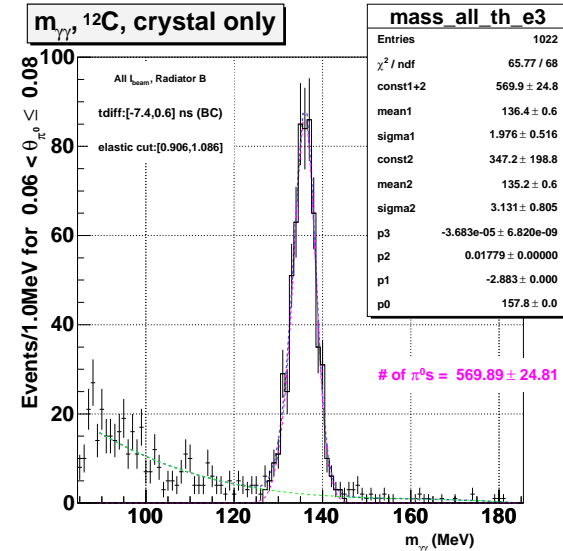


## Analysis Details: $\pi^0$ Yield Extraction

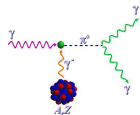
### Extracting Elastic Pion Yields versus $\theta_{\pi^0}$



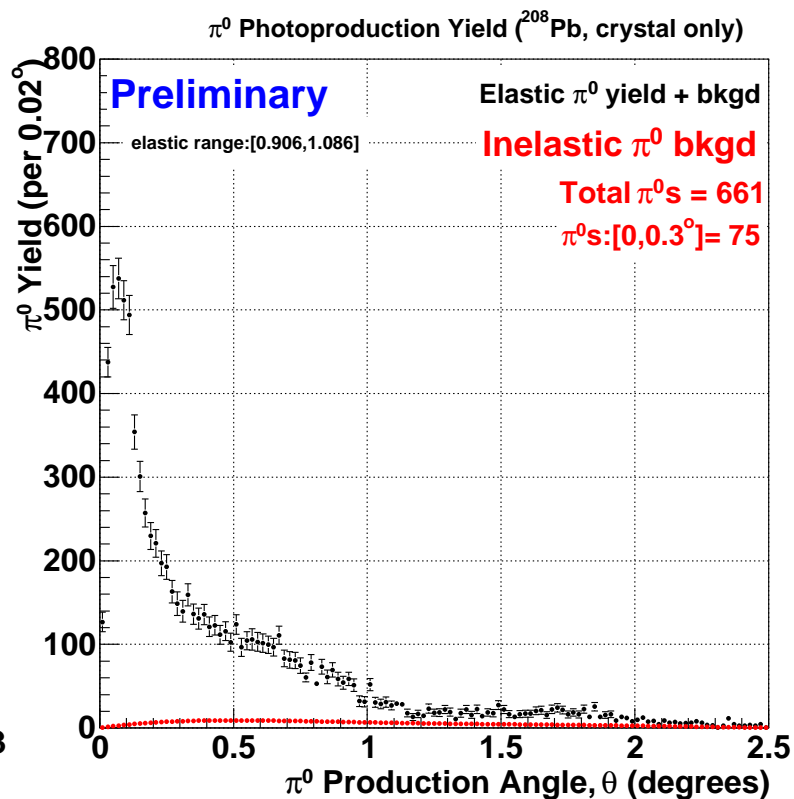
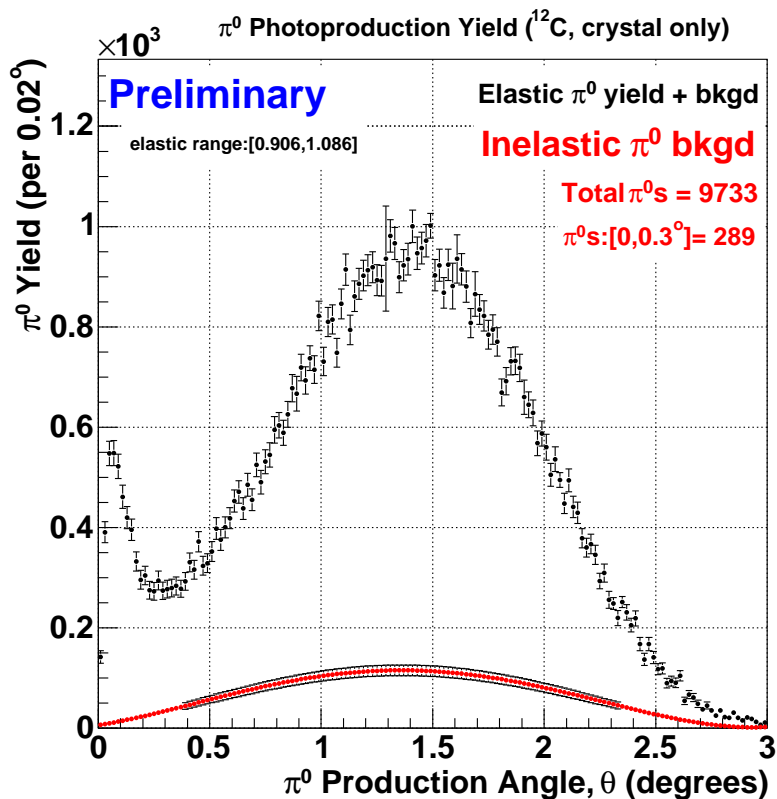
- For each  $\theta_{\pi^0}$  bin, apply elastic cut and form  $m_{\gamma\gamma}$  distributions; perform fit and extract peak counts = uncorrected yield.
- Correct for inelastic bkgd by evaluating  $\pi^0$  elasticity distribution explicitly for each  $\theta_{\pi^0}$ ; evaluate inelastic bkgd under the elastic peak using fit and subtract from yield.

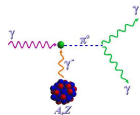




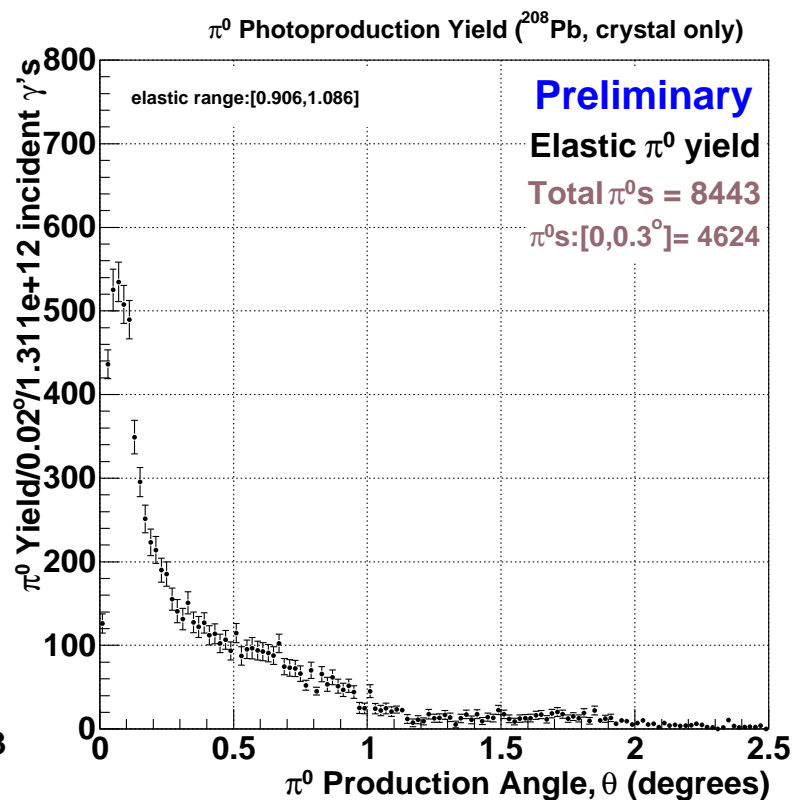
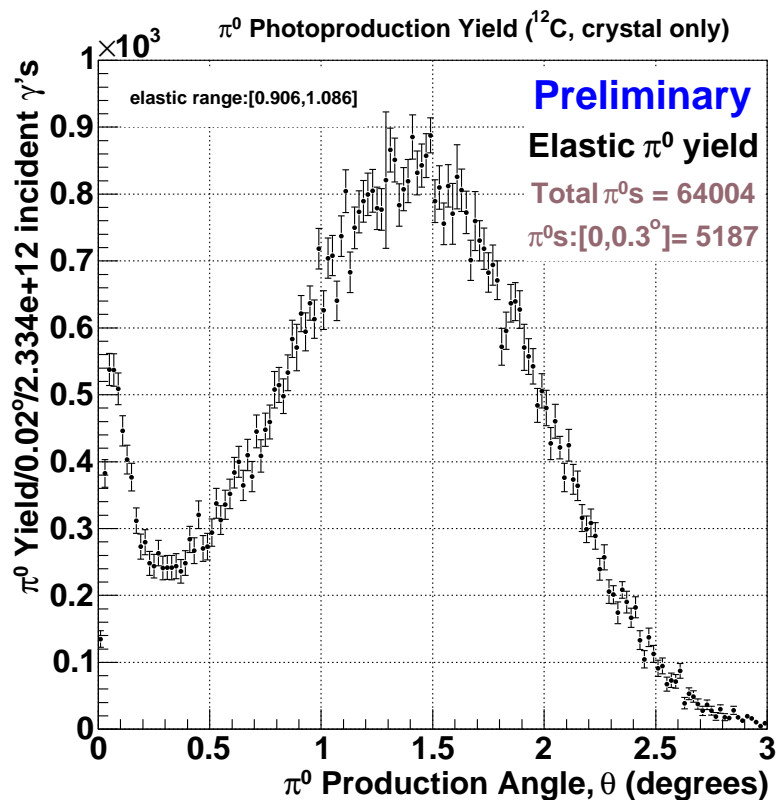


## Analysis Details: Yield Result for $^{12}\text{C}$ and $^{208}\text{Pb}$





## Yield Results for $^{12}\text{C}$ and $^{208}\text{Pb}$





## Analysis Details: $\Gamma_{\pi^0 \rightarrow \gamma\gamma}$ Determination

- Convert Yield to Cross Section.

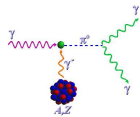
$$\frac{d\sigma_{exp}}{d\theta_{\pi^0}} = \frac{N_{\pi^0}^{yield}(\theta_{\pi^0})}{N_{\gamma} \times N_t \times \epsilon_{\pi^0}(\theta_{\pi^0}) \times \Delta\theta_{\pi^0}} \quad (7)$$

- where  $N_{\gamma} \equiv$  # of  $\gamma$ 's on target (uncertainty  $\sim 1.1\%$ ).
- where  $N_t \equiv$  target atoms/cm<sup>2</sup> (thickness mapped to  $\sim 0.05\%$ ).
- where  $\epsilon_{\pi^0} \equiv$  experimental acceptance (uncertainty  $\sim 0.6\%$ ).

- Fit experimental data with parameterization:

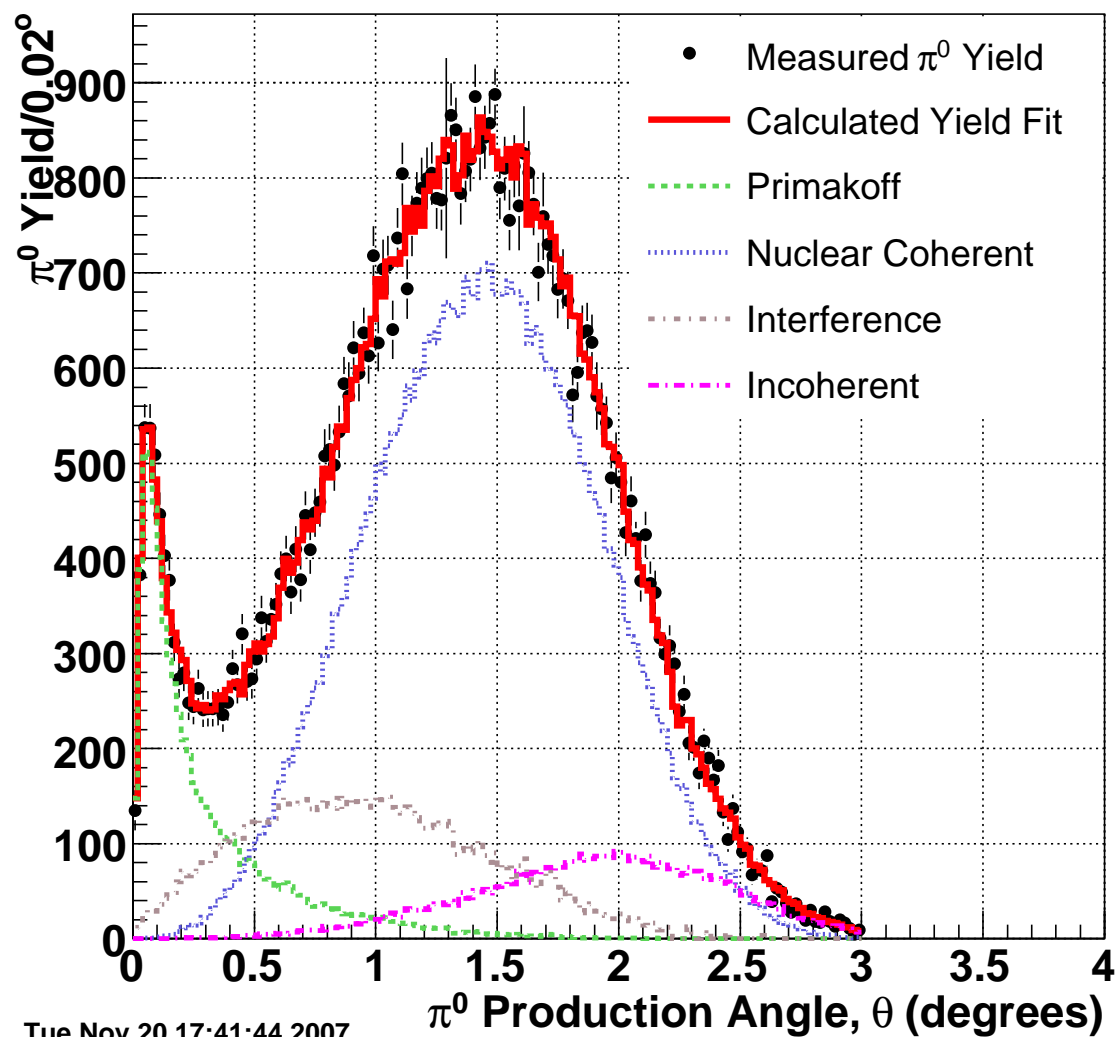
$$\frac{d\sigma_{exp}}{d\theta_{\pi^0}} = b_p \frac{d\sigma_P}{d\Omega} + b_c \frac{d\sigma_N}{d\Omega} + b_i \frac{d\sigma_I}{d\Omega} + 2\cos\phi \sqrt{b_p b_c \frac{d\sigma_P}{d\Omega} \frac{d\sigma_C}{d\Omega}} \quad (8)$$

- where the parameter  $b_p = \Gamma_{\gamma\gamma}$
- Vary the four parameters ( $b_p$ ,  $b_c$ ,  $b_i$ , and  $\phi$ ) and minimize  $\chi^2$ .

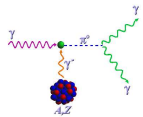


## $^{12}\text{C}$ Target Yield Fit

Preliminary  $\pi^0$  Photoproduction yield ( $^{12}\text{C}$ , crystal only)

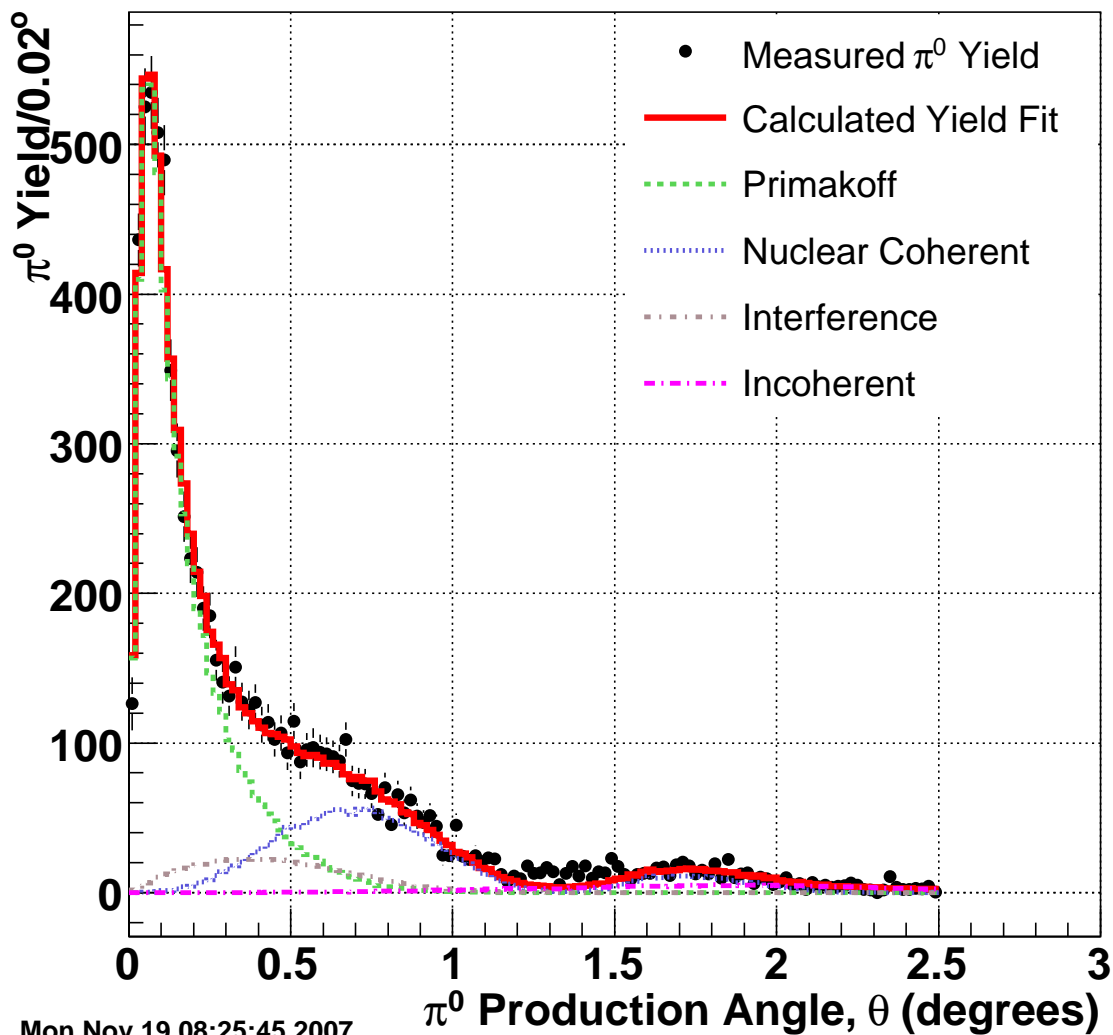


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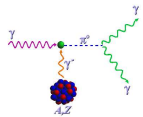


## $^{208}\text{Pb}$ Target Yield Fit

Preliminary  $\pi^0$  Photoproduction yield ( $^{208}\text{Pb}$ , crystal only)



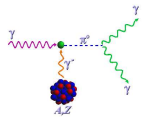
Mon Nov 19 08:25:45 2007



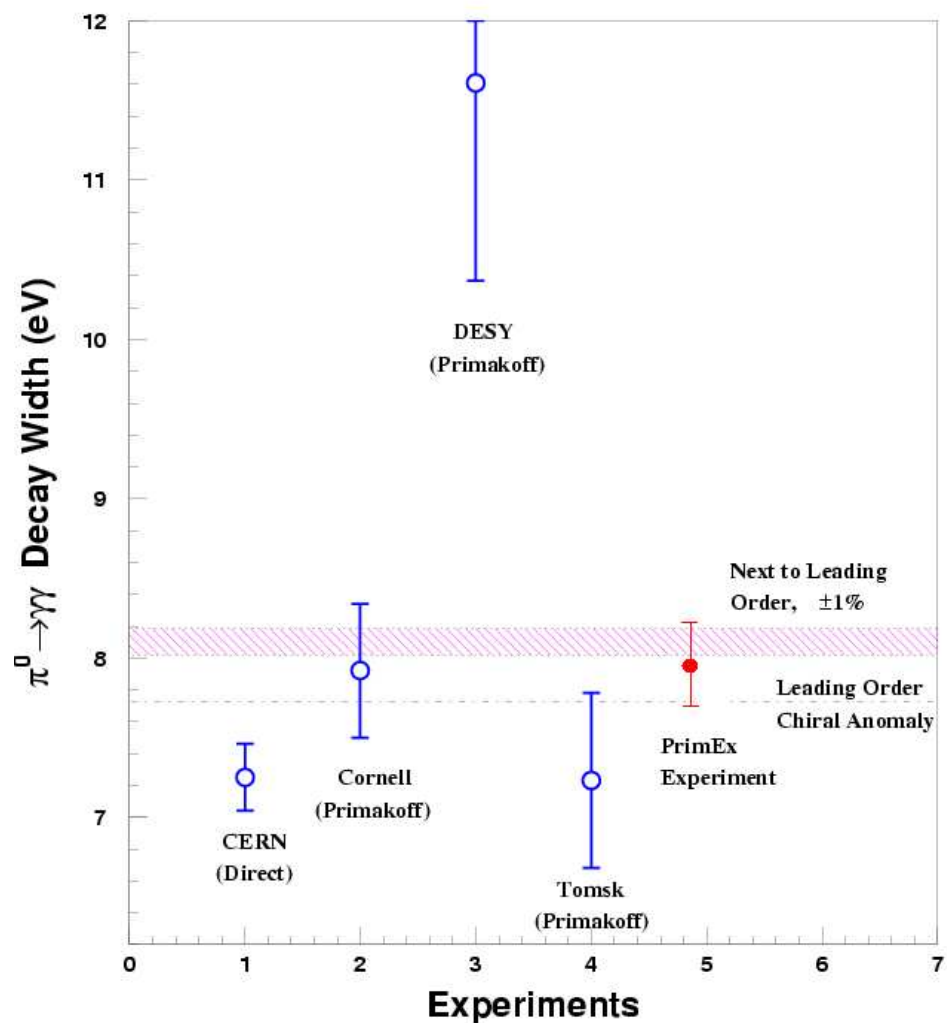
## Systematic Error Table and Yield Fit Result

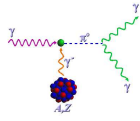
$m_{\gamma\gamma}$ fits + inelast bkgd corr.	$\pm 1.0$
Inelastic bkgd shape uncert.	$\pm 0.75$
Photon flux	$\pm 1.1$
Incoherent XS shape uncert.	$\pm 1.3$
Nuclear coh. XS energy dep.	$\pm 0.04$
Detection/Recon efficiency	$\pm 0.5$
Fiducial Acceptance	$\pm 0.3$
Event Selection	$\pm 1.0$
Target thick. + branch ratio	$\pm 0.06$
Tagged Photon Energy	$\pm 0.1$
Total Systematic	$\pm 2.4\%$

**Prelim. Result:**  $\Gamma_{\pi^0 \rightarrow \gamma\gamma} = 7.93\text{eV} \pm 1.6\% (\text{stat}) \pm 2.4\% (\text{syst})$



## $\Gamma_{\pi^0 \rightarrow \gamma\gamma}$ Preliminary Result





## Summary and Outlook

- High Quality precision  $\pi^0$  photoproduction data on  $^{12}\text{C}$  and  $^{208}\text{Pb}$  targets using  $4.9 \leq E_{\gamma}^{\text{tagged}} \leq 5.5$  GeV has been collected and analyzed by the PrimEx Collaboration.
- Preliminary cross section results from studied calibration reactions  $e^+e^-$  production and Compton scattering are both in excellent agreement with theory (at the 2 – 3% level).
- All three  $\sim$ independent  $\pi^0$  analysis groups have achieved very consistent results.
- The preliminary  $\pi^0$  partial width result from this analysis:  
 $\Gamma_{\pi^0 \rightarrow \gamma\gamma} = 7.93\text{eV} \pm 1.6\%(\text{stat}) \pm 2.4\%(\text{syst})$ .
- The mean lifetime:  $(8.20 \pm 0.24) \times 10^{-17}$  s
- Preliminary  $\Gamma_{\pi^0 \rightarrow \gamma\gamma}$  results from both targets in excellent agreement.
- Continued work on reducing systematic error and finalizing results.