

PMT Non-Linearity Studies at ISU

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February 25, 2018



Outline

- Introduction and Motivation
- Linearity Test Apparatus
- Light Level Selection
- Measurement and Analysis Techniques
- Results and Summary

Introduction (What is Asymmetry? What is non-linearity)?

LED

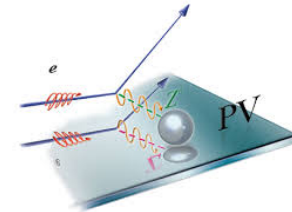
$$A_{LED} = \frac{N^+ - N^-}{N^+ + N^-} \quad \text{With, } N_{avg} = \frac{N^+ + N^-}{2}$$

$A_{LED} = A_{true} (1 + \beta N_{avg})$ is the fit function.

- $N^\pm = N_S^\pm (1 + \beta N_S^\pm)$ is the PMT response for the signal N_S^\pm .
- β parameterizes the non-linearity
- N_{avg} settings provided by ND filter wheel
- Fits to A_{LED} vs. N_{avg} plot give A_{true} and $A_{true} \beta$ and hence the non-linearity.
- Linearity measurement plays an important role in detector systematics.
- R7723Q PMT with modified base for improved non-linearity was used.

PREx-II/CREx

- Polarized beam with unpolarized target.
- Measurements in opposite helicity states.
- Asymmetry of cross sections:

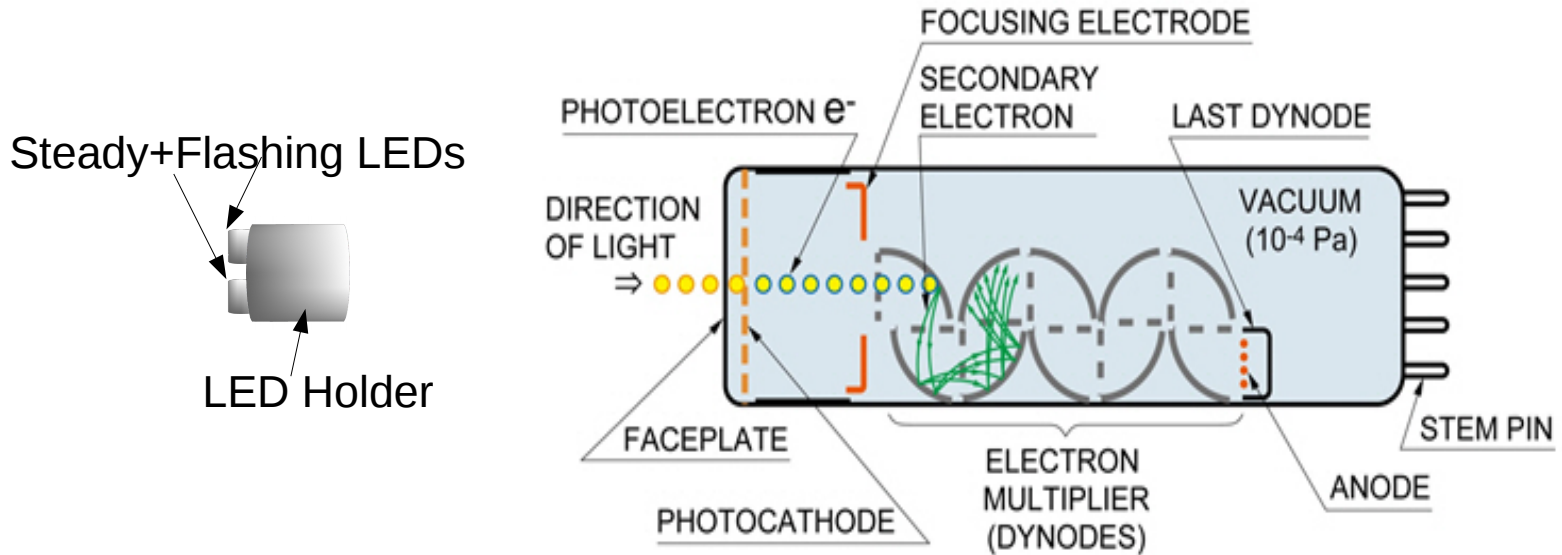


$$A_{pv} = \frac{\sigma_R - \sigma_L}{\sigma_R + \sigma_L}$$

$$\sigma_{R(L)} = \frac{d\sigma_{R(L)}}{d\Omega} \propto (S_y + S_z^{R(L)})^2$$

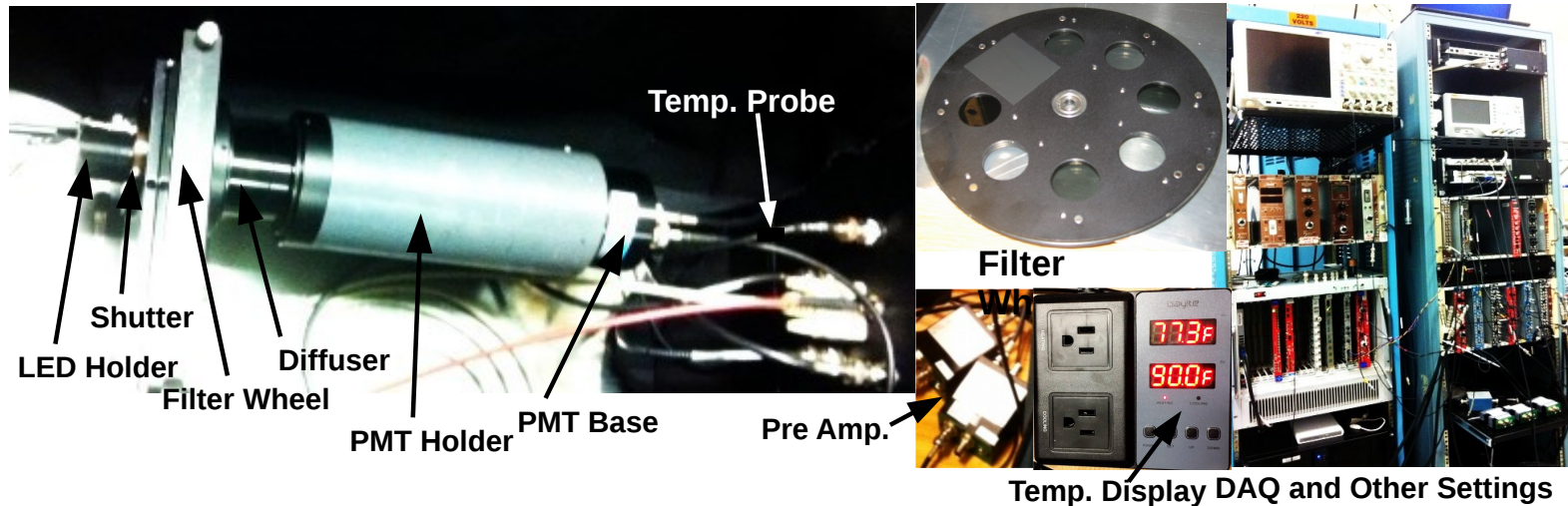
$$\propto \frac{\begin{array}{c} \text{Z}^0 \\ \text{Y} \end{array}}{2} \sim \frac{10^{-4} Q^2}{\text{GeV}^2}$$

Why Linearity Study is Important for PREx-II/CREx?



- PMTs tested here will be used in the PREx-II/CREx detectors
- PMT non-linearity is an important systematic error and needs to be understood well before experiment
- The systematic error budget for detector non-linearity is 0.3 % (CREx) and 1 % (PREx-II)

Linearity Test Box And Integrating DAQ



- LED Holder → holds two LEDs, each with 2 mm diameter collimation
- Electronic Shutter → has now been connected with a relay to turn it “ON” and “OFF” automatically at any interval with computer script
- Filter Wheel → Computer Controlled Edmund Optics’ Absorptive ND filters (400-700 nm) with 8 (100, 79, 63, 50, 40, 25, 10, 1)% transmission settings (~randomly ordered)
- Filter Wheel is now controlled automatically using a shell script
- UV Diffuser → Edmund Optics’ ground fused silica
- PMT Holder → 2” PMT with modified base for improved linearity
- Different pre-Amp settings with different resistances and offsets tested (MAIN, LUMI, KDPA, and SNS)

Maintaining Temperature Stability of Apparatus During Measurements

- ➔ Temperature probe has been installed inside the linearity test box in order to monitor the air temperature near PMT base.
- ➔ We now turn on HV at least 24 hrs before taking data – helps stabilize PMT temperature (with smaller fluctuation during data taking).
- ➔ After changing HV, we now wait at least 15-20 minutes before starting next run (helps in temperature stabilization).

Apparatus Improvements

- Now the LED, Trigger, and Gate timings have been controlled through HAPPEX Timer board.
- Light level (LL) has now been calibrated using DAC16, which improves the resolution in LL selection.
- Need to calibrate picoammeter used for LL measurement.
- Need to get unity gain base for R7723Q.

Qweak ADC Details

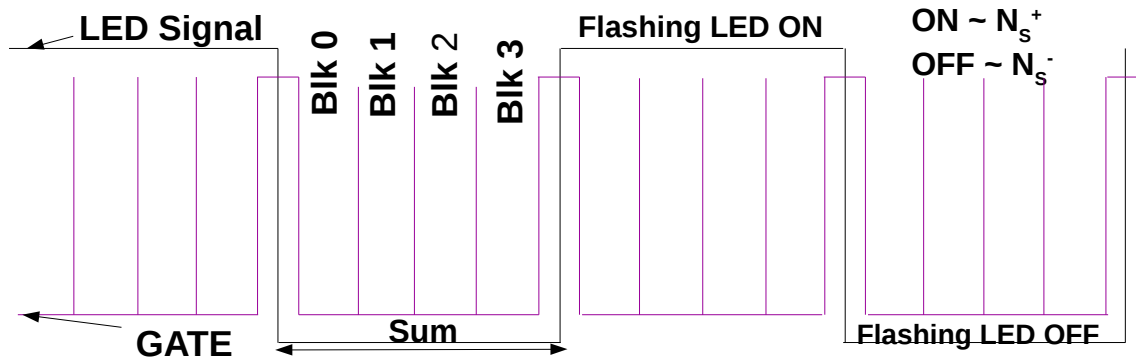


Figure: DAQ response sampled in four blocks.

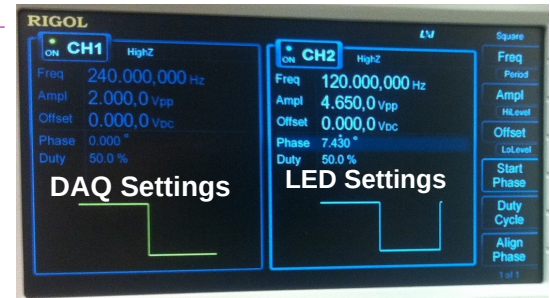


Figure: Function Generator settings.

- Samples the voltage every 2 μ s
- Has a ± 10 V range with 18 bit resolution (corresponding to 76.29 μ V/channel)
- Has 8 inputs with 12 Ω input impedance
- Working with CODA 2.6.2 and a Linux ROC
- We use a Struck SIS3610 for triggering
- Each GATE is split into 4 blocks with the length (in time) of each block specified by user
- For 120 Hz flipping rate, we set 500 samples/block. So 2000 total samples, every 2 μ s, gives 8000 μ s long gate
- We are currently using a function generator to provide synchronized DAQ and LED driver signals

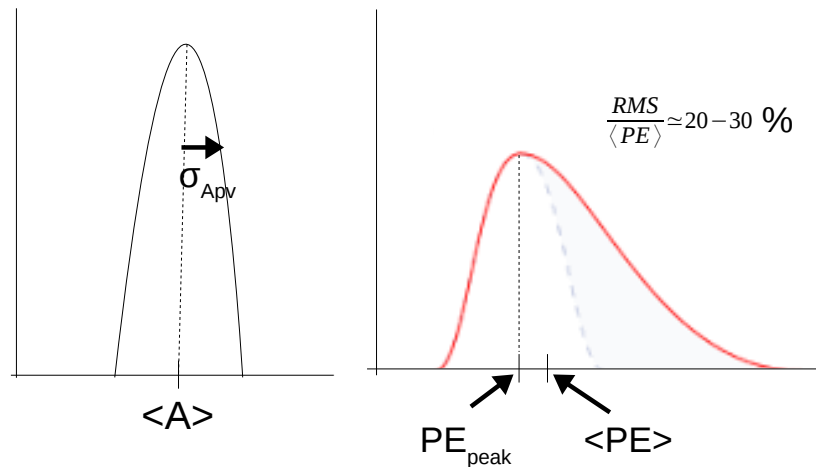
Light Level $\iff I_{cathode}$

- Used constant LED
- Used unity gain PMT (R375)
- Used DAC 16 for constant LED
- Used pico-ammeter to measure I_c which is effectively I_{PE} because gain is 1
- QE of R375 PMT is different but similar to R7723Q PMT. Planning to get unity gain base for R7723Q PMT
- PMTs should show the best linear response with the LL equivalent to Cerenkov light that it receives during PREx-II/CREx

Light Level Validation During Commissioning

- Set HVs to our expected best values
- Collect “production” data
- Infer LL from measured Asymmetry width (σ_{Apv}):

$$rate = \frac{fliprate}{2(\sigma_{Apv})^2} \left[1 + \underbrace{\left(\frac{RMS}{\langle PE \rangle} \right)^2}_{\text{Excess Noise}} \right]$$



- $LL \equiv I_c = rate \times PE_{peak} \times 1.602 \times 10^{-19}$
- Can also check for consistency between up-and down-stream widths for each arm separately and between the two arms.

Selection of Light Levels to Test

PREx PE-Distribution

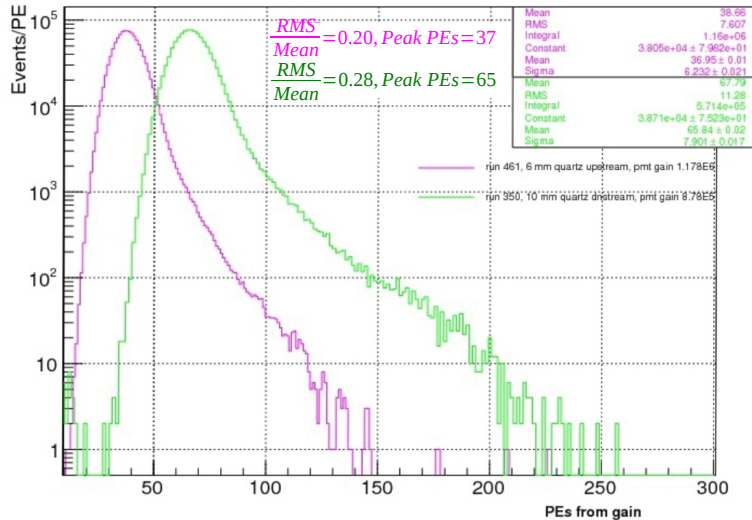


Photo-Electron Distribution - simulated vs real data

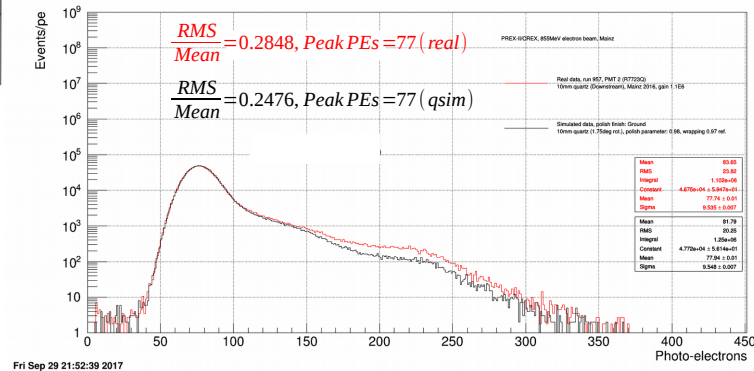


Figure: Produced by Carlos Bula

PREx-II

- Rate = 1 GHz
- LL for upstream quartz = $1\text{GHz} \cdot 37 \cdot e \sim 6 \text{ nA}$
- LL for downstream quartz $\sim 10 \text{ nA}$ (65 peak PEs)

→ Tested 3 PMTs so far

CREx

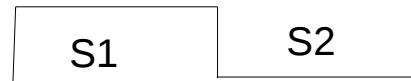
- Rate = 50 MHz
- LL for upstream quartz = $50\text{MHz} \cdot 37 \cdot e \sim 0.3 \text{ nA}$
- LL for downstream quartz $\sim 0.5 \text{ nA}$ (65 peak PEs)

Steps in Data Collection

- ♦ LL controlled by HAPPEX timer DAC16, calibrated using R375 PMT with unity gain base
- ♦ DAQ (240 Hz) and LED flash (120 Hz) signals were synchronized
- ♦ Proper timing setting between LED, TRIGGER and GATE (45 μ s and 100 μ s respectively) was maintained (GATE duration is 8000 μ s and the GATE does not start until 20 μ s after the ADC receives the GATE signal)
- ♦ An automated filter wheel and shutter script orchestrated the data collection over 20 cycles of filter wheel:
 - Each filter stayed in its position for 10 sec and during each filter change the shutter remains closed for 2 sec
 - Just before each new filter cycle, pedestal data was taken for 5sec
 - Asymmetry Mean and Error from 20 cycles of filter wheel was used to produce non-linearity plot (A_{LED} vs N_{avg})

Steps and Approaches in Data Analysis

- Used simplified version of vQwk Analyzer to analyze data
- An automated c++ code has been developed that removes any “unclean” data during filter rotation and analyzes the rest
- The data from two consecutive gates were used to calculate simple pair-wise asymmetry

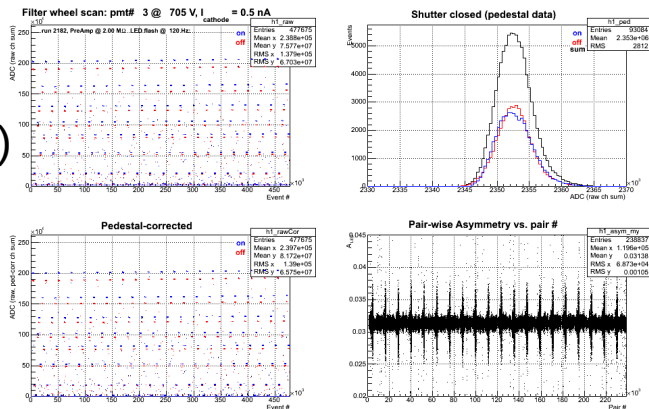


$$A = \frac{S_1 - S_2}{S_1 + S_2}$$

Measurement Steps

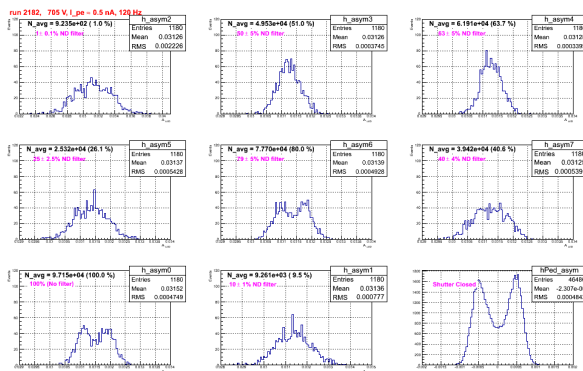
- Take data with 120 Hz of flipping rate for 20 cycles of filter wheel rotation.
- Subtract pedestal, and find pairwise asymmetry.

(1)



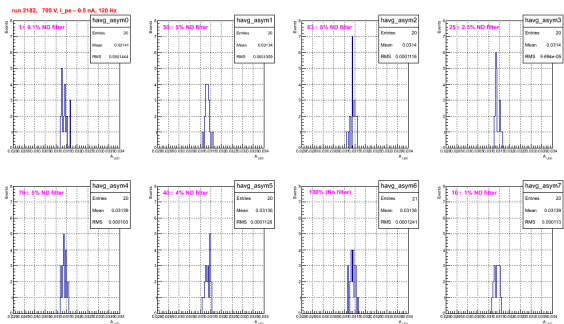
- Plot asymmetry for individual filter setting.
- Find the mean and RMS for each plots.

(2)



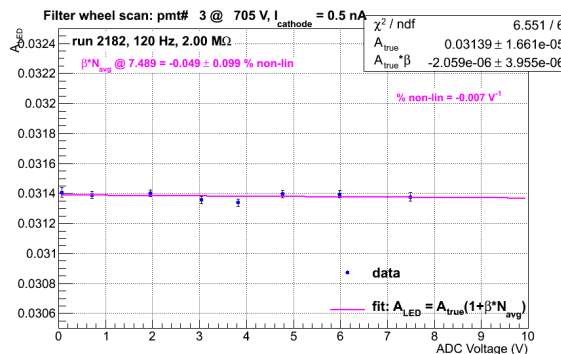
- Plot the mean asymmetry for each filter setting.
- Find the mean and RMS for all 20 cycles.

(3)

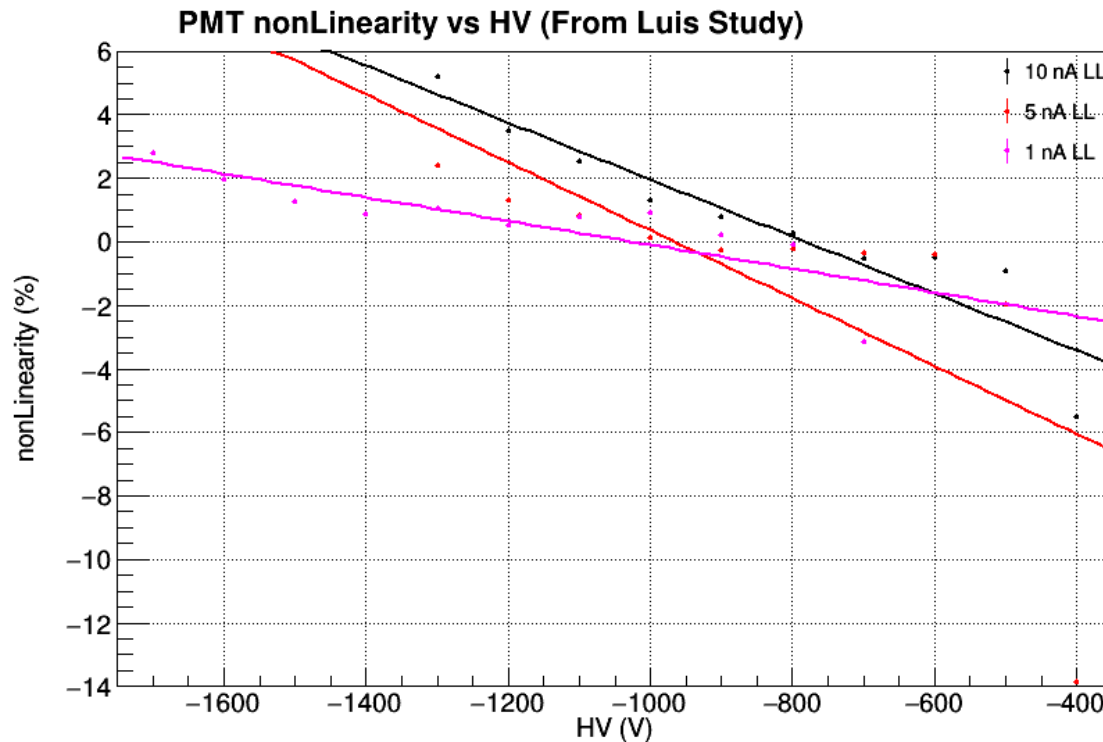


- Plot the mean asymmetry vs ADC Voltage for each filter setting.
- Linear fit the data points calculate slope and hence non-linearity

(4)



Linearity Study in the Past



LL = 10 nA

HV	I_{out}	nonLin
-400	0.54	-5.5
-500	1.56	-0.9
-600	3.7	-0.48
-700	7.8	-0.54
-800	15	0.28
-900	26	0.78
-1000	43	1.32
-1100	68	2.52
-1200	104	3.48
-1300	155	5.2

LL = 5 nA

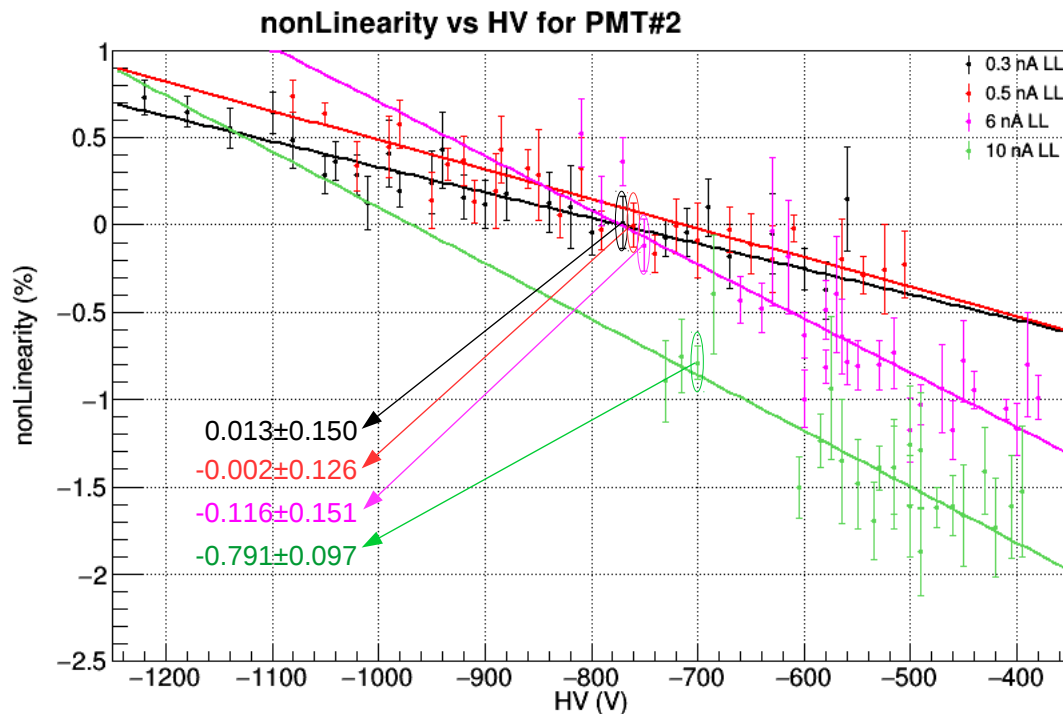
HV	I_{out}	nonLin
-400	0.26	-13.85
-500	0.76	-1.96
-600	1.8	-0.39
-700	3.8	-0.34
-800	7.2	-0.21
-900	12.6	-0.26
-1000	20.7	0.11
-1100	32.4	0.82
-1200	48.5	1.29
-1300	70	2.41

LL = 1 nA

HV	I_{out}	nonLin
-700	0.75	-3.15
-800	1.4	-0.075
-900	2.5	0.23
-1000	4.1	0.93
-1100	6.3	0.79
-1200	9.4	0.51
-1300	13.5	1.03
-1400	18.8	0.88
-1500	26.3	1.27
-1600	34	1.98
-1700	44	2.79

Figure: Reproduced From Luis Mercado's Dissertation.

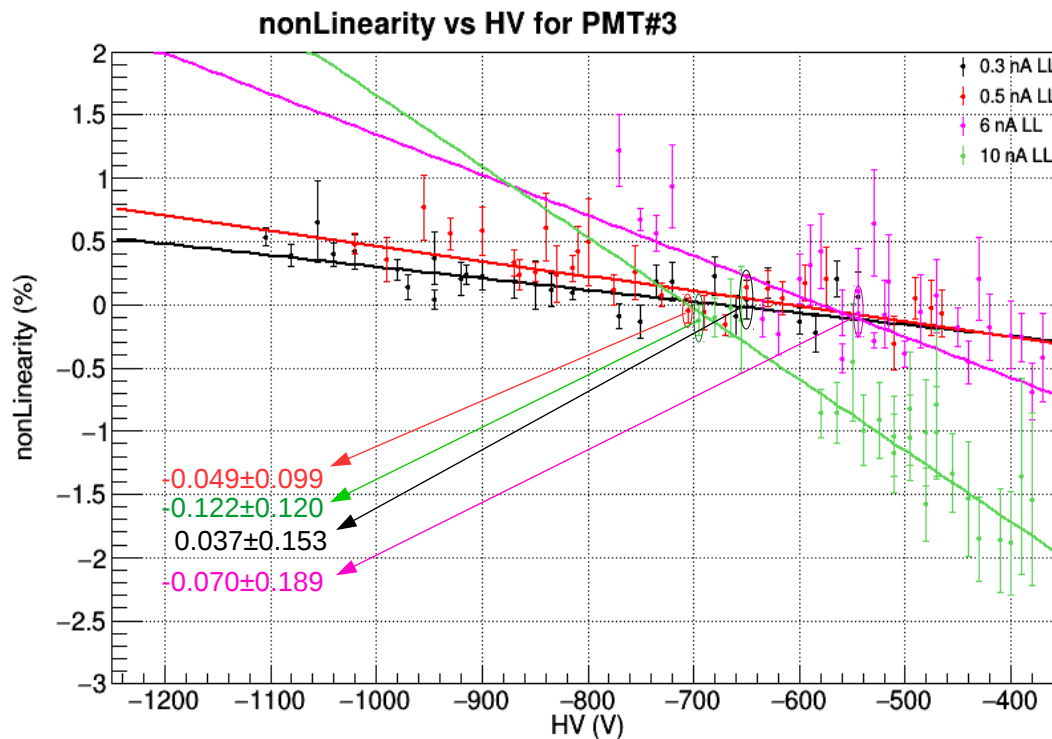
Summary for PMT#2



LL = 0.3 nA						LL = 6.0 nA					
Run	HV	PreAmp	non-Linear	Error	$\chi^2/6df$	Run	HV	PreAmp	non-Linear	Error	$\chi^2/6df$
1938	-1220	0.3	0.729	0.100	4.872	2073	-810	0.1	0.526	0.194	26.24
1939	-1180	0.3	0.648	0.089	2.709	2074	-790	0.1	0.137	0.138	16.51
1940	-1140	0.3	0.552	0.113	5.997	2075	-770	0.1	0.360	0.138	4.003
1941	-1100	0.3	0.645	0.119	7.070	2076	-750	0.1	-0.116	0.151	10.63
1947	-1080	0.5	0.483	0.161	8.400	2050	-660	0.3	-0.429	0.135	6.789
1948	-1050	0.5	0.287	0.106	3.625	2046	-640	0.3	-0.475	0.140	15.70
1949	-1020	0.5	0.286	0.113	9.049	2047	-630	0.3	-0.037	0.424	85.80
1950	-990	0.5	0.409	0.193	12.29	2048	-615	0.3	-0.182	0.326	41.56
1933	-1040	0.6	0.366	0.114	4.405	2056	-600	0.5	-0.996	0.163	12.75
1934	-1010	0.6	0.129	0.153	12.35	2057	-580	0.5	-0.488	0.170	11.90
1935	-980	0.6	0.197	0.096	2.246	2058	-570	0.5	-0.398	0.334	65.96
1936	-950	0.6	0.243	0.179	13.31	2059	-560	0.5	-0.787	0.131	9.769
1952	-940	1.0	0.430	0.218	18.58	2052	-600	0.6	-0.631	0.133	11.49
1953	-920	1.0	0.160	0.127	7.389	2053	-580	0.6	-0.814	0.096	6.912
1954	-900	1.0	0.119	0.140	8.746	2054	-565	0.6	-0.640	0.215	26.28
1955	-880	1.0	0.180	0.150	5.322	2055	-550	0.6	-0.805	0.141	7.201
1957	-840	2.0	0.129	0.170	8.034	2060	-530	1.0	-0.803	0.144	19.21
1958	-820	2.0	0.106	0.237	10.61	2061	-515	1.0	-0.733	0.201	33.30
1959	-800	2.0	-0.042	0.132	4.793	2062	-500	1.0	-1.174	0.182	12.41
1960	-770	2.0	0.013	0.150	7.264	2063	-490	1.0	-1.027	0.114	4.954
1961	-730	4.0	-0.075	0.104	3.345	2064	-470	2.0	-0.938	0.253	28.87
1962	-710	4.0	-0.042	0.136	4.074	2065	-460	2.0	-1.176	0.169	22.99
1963	-690	4.0	0.099	0.166	5.990	2066	-450	2.0	-0.780	0.234	24.39
1964	-670	4.0	-0.180	0.180	3.660	2067	-440	2.0	-0.944	0.108	7.177
1943	-630	10.0	-0.050	0.230	10.84	2068	-410	4.0	-1.054	0.057	1.070
1944	-600	10.0	-0.252	0.116	1.585	2070	-400	4.0	-1.169	0.150	9.485
1945	-580	10.0	-0.374	0.162	3.719	2071	-390	4.0	-0.800	0.297	36.38
1946	-560	10.0	0.148	0.299	10.35	2072	-380	4.0	-0.990	0.127	7.438

LL = 0.5 nA						LL = 10.0 nA					
Run	HV	PreAmp	non-Linear	Error	$\chi^2/6df$	Run	HV	PreAmp	non-Linear	Error	$\chi^2/6df$
1991	-1080	0.3	0.739	0.093	1.902	2102	-730	0.1	-0.893	0.233	17.05
1992	-1050	0.3	0.638	0.058	1.598	2103	-715	0.1	-0.750	0.212	18.20
1993	-1020	0.3	0.337	0.139	9.607	2104	-700	0.1	-0.791	0.095	4.500
1994	-990	0.3	0.445	0.177	9.531	2105	-685	0.1	-0.398	0.341	70.38
1982	-980	0.5	0.574	0.137	6.722	2098	-605	0.3	-1.504	0.178	11.27
1983	-950	0.5	0.141	0.159	14.17	2099	-585	0.3	-1.236	0.154	13.39
1984	-920	0.5	0.369	0.143	7.609	2100	-575	0.3	-0.934	0.408	102.2
1986	-890	0.5	0.196	0.216	12.08	2101	-565	0.3	-1.354	0.357	49.27
1995	-935	0.6	0.345	0.091	4.216	2088	-550	0.5	-1.484	0.256	42.98
1996	-910	0.6	0.132	0.123	8.034	2089	-535	0.5	-1.694	0.224	32.93
1997	-885	0.6	0.432	0.194	19.43	2090	-515	0.5	-1.448	0.296	46.25
1998	-860	0.6	0.321	0.110	8.270	2091	-500	0.5	-1.260	0.339	24.36
1987	-850	1.0	0.284	0.260	27.48	2093	-530	0.6	-1.391	0.128	9.687
1988	-830	1.0	0.054	0.125	5.673	2094	-515	0.6	-1.386	0.272	41.63
1989	-810	1.0	0.322	0.180	12.91	2096	-500	0.6	-1.611	0.290	50.45
1990	-790	1.0	-0.031	0.113	6.962	2097	-490	0.6	-1.874	0.252	34.81
1972	-760	2.0	-0.002	0.126	5.791	2083	-490	1.0	-1.288	0.329	71.75
1973	-740	2.0	-0.165	0.110	2.221	2084	-475	1.0	-1.618	0.117	8.316
1974	-720	2.0	-0.008	0.157	6.458	2085	-460	1.0	-1.609	0.171	18.30
1975	-700	2.0	-0.092	0.214	20.77	2086	-450	1.0	-1.666	0.292	38.59
1967	-670	4.0	-0.026	0.132	3.998	2079	-430	2.0	-1.409	0.246	36.01
1968	-650	4.0	-0.108	0.172	8.149	2080	-420	2.0	-1.731	0.284	31.41
1969	-630	4.0	-0.197	0.189	5.280	2081	-405	2.0	-1.613	0.293	79.77
1970	-610	4.0	-0.019	0.076	1.627	2082	-395	2.0	-1.529	0.375	67.14
1976	-565	10.0	-0.195	0.232	16.88						
1978	-545	10.0	-0.286	0.106	2.188						
1979	-525	10.0	-0.253	0.254	10.81						
1980	-505	10.0	-0.224	0.190	4.669						

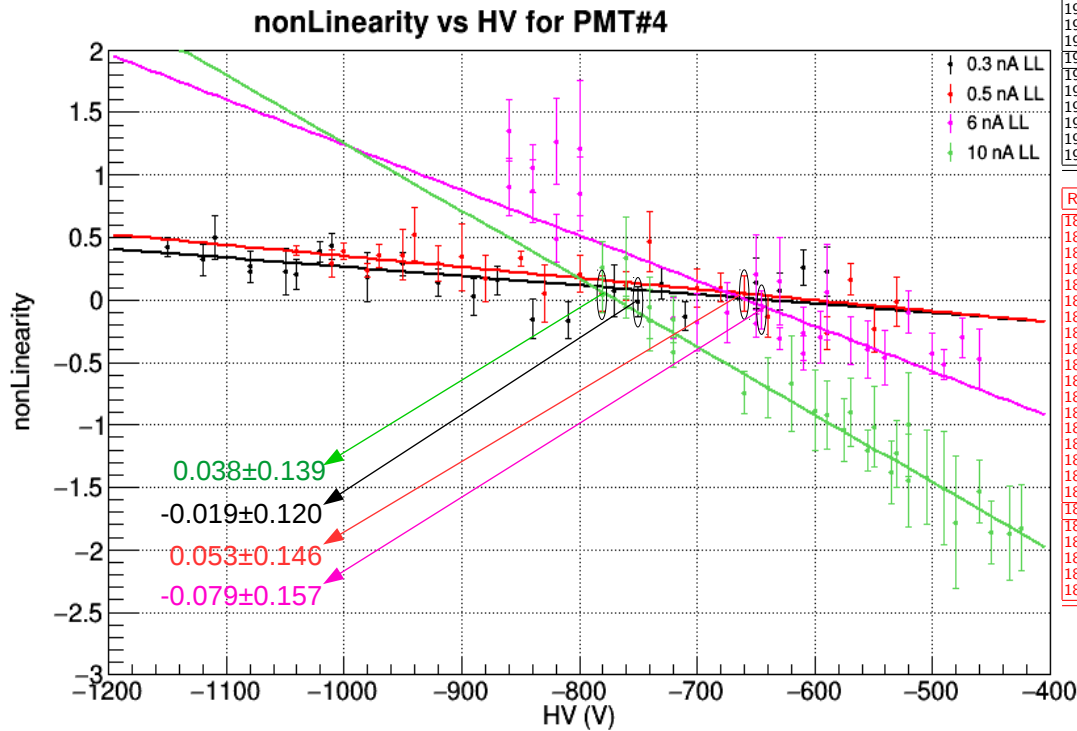
Summary for PMT#3



LL = 0.3 nA					LL = 6.0 nA						
Run	HV	PreAmp	non-Lin	Error	$\chi^2/6df$	Run	HV	PreAmp	non-Lin	Error	$\chi^2/6df$
2242	-1105	0.3	0.538	0.070	2.229	2154	-770	0.1	1.221	0.282	29.33
2245	-1080	0.3	0.392	0.085	2.630	2155	-750	0.1	0.672	0.086	4.787
2244	-1055	0.3	0.655	0.323	78.83	2157	-735	0.1	0.564	0.140	4.744
4246	-1040	0.3	0.396	0.089	3.307	2158	-720	0.1	0.936	0.331	63.63
2232	-1020	0.5	0.418	0.132	6.555	2144	-635	0.3	-0.115	0.140	6.057
2233	-980	0.5	0.277	0.084	3.254	2177	-620	0.3	-0.230	0.170	10.59
2236	-945	0.5	0.366	0.206	21.98	2147	-600	0.3	0.205	0.195	19.37
2235	-915	0.5	0.239	0.073	3.526	2148	-590	0.3	0.318	0.317	56.22
2237	-970	0.6	0.144	0.099	4.944	2163	-580	0.5	0.419	0.296	42.13
2238	-945	0.6	0.041	0.073	4.265	2164	-560	0.5	-0.426	0.116	8.968
2239	-920	0.6	0.205	0.134	9.197	2165	-545	0.5	0.110	0.334	23.33
2240	-900	0.6	0.231	0.119	2.264	2166	-530	0.5	0.645	0.418	42.82
2228	-870	1.0	0.181	0.133	8.208	2149	-560	0.6	-0.063	0.184	23.28
2229	-850	1.0	0.157	0.191	12.07	2150	-545	0.6	-0.070	0.189	7.863
2230	-835	1.0	0.114	0.133	11.41	2151	-530	0.6	-0.285	0.060	2.140
2231	-815	1.0	0.093	0.047	0.778	2153	-520	0.6	-0.076	0.266	62.65
2209	-770	2.0	-0.094	0.098	5.369	2159	-515	1.0	0.181	0.377	103.7
2211	-750	2.0	-0.132	0.132	11.97	2160	-500	1.0	-0.389	0.104	2.674
2212	-735	2.0	0.182	0.132	6.689	2161	-485	1.0	-0.053	0.291	55.89
2215	-720	2.0	0.187	0.152	16.48	2262	-470	1.0	0.069	0.289	29.13
2217	-680	4.0	0.226	0.151	11.18	2173	-450	2.0	-0.178	0.150	6.963
2218	-660	4.0	-0.089	0.165	14.11	2174	-440	2.0	-0.456	0.169	14.42
2219	-650	4.0	0.037	0.153	8.451	2175	-430	2.0	0.205	0.323	49.87
2220	-630	4.0	0.171	0.121	6.446	2176	-420	2.0	-0.175	0.260	47.61
2222	-600	10.0	-0.130	0.104	4.948	2167	-400	4.0	-0.240	0.265	21.39
2226	-585	10.0	-0.219	0.155	8.466	2168	-390	4.0	-0.258	0.189	23.87
2224	-565	10.0	0.206	0.138	12.54	2169	-380	4.0	-0.686	0.225	16.90
2245	-545	10.0	0.064	0.190	20.87	2171	-370	4.0	-0.417	0.348	41.25

LL = 0.5 nA					LL = 10.0 nA						
Run	HV	PreAmp	non-Lin	Error	$\chi^2/6df$	Run	HV	PreAmp	non-Lin	Error	$\chi^2/6df$
2199	-1020	0.3	0.481	0.084	1.706	2122	-695	0.1	-0.122	0.120	10.38
2200	-990	0.3	0.360	0.173	14.46	2123	-680	0.1	-0.102	0.154	12.09
2201	-955	0.3	0.768	0.260	24.63	2124	-665	0.1	-0.024	0.230	30.21
2203	-930	0.3	0.562	0.124	11.19	2125	-655	0.1	-0.118	0.422	90.98
2191	-900	0.5	0.585	0.192	19.69	2130	-580	0.3	-0.860	0.189	20.04
2192	-865	0.5	0.234	0.121	5.292	2131	-565	0.3	-0.856	0.239	44.46
2193	-840	0.5	0.614	0.263	38.23	2142	-550	0.3	-0.455	0.465	104.3
2194	-815	0.5	0.287	0.104	8.041	2133	-540	0.3	-0.993	0.282	34.38
2195	-870	0.6	0.331	0.104	5.364	2138	-525	0.5	-0.913	0.302	44.65
2196	-850	0.6	0.261	0.080	2.051	2139	-510	0.5	-1.177	0.307	52.93
2197	-830	0.6	0.243	0.228	30.84	2140	-495	0.5	-0.818	0.448	111.9
2198	-810	0.6	0.424	0.199	24.35	2141	-480	0.5	-1.012	0.422	89.00
2186	-800	1.0	0.495	0.347	59.59	2126	-510	0.6	-1.040	0.313	74.72
2187	-775	1.0	0.120	0.118	11.18	2127	-495	0.6	-1.051	0.343	70.39
2188	-755	1.0	0.257	0.214	17.96	2128	-480	0.6	-1.578	0.289	60.84
2189	-730	1.0	0.078	0.097	3.404	2129	-470	0.6	-1.004	0.356	93.44
2182	-705	2.0	-0.049	0.099	6.551	2134	-470	1.0	-0.793	0.590	274.1
2183	-690	2.0	-0.062	0.134	8.123	2135	-455	1.0	-1.332	0.311	90.87
2183	-670	2.0	-0.161	0.081	4.227	2136	-440	1.0	-1.537	0.457	182.0
2184	-650	2.0	0.144	0.092	4.583	2137	-430	1.0	-1.853	0.333	37.05
2178	-630	4.0	0.132	0.143	12.57	2118	-410	2.0	-1.865	0.411	89.17
2179	-616	4.0	0.049	0.130	8.470	2119	-400	2.0	-1.884	0.408	133.3
2180	-595	4.0	0.175	0.140	17.19	2120	-390	2.0	-1.358	0.772	241.9
2181	-575	4.0	0.204	0.249	27.52	2121	-380	2.0	-1.541	0.684	318.1
2205	-510	10.0	-0.305	0.214	36.31						
2206	-490	10.0	0.052	0.160	11.41						
2207	-475	10.0	-0.024	0.215	19.85						
2208	-465	10.0	-0.067	0.187	12.06						

Summary for PMT#4



LL = 0.3 nA					LL = 6.0 nA						
Run	HV	PreAmp	non-Lin	Error	$\chi^2/6df$	Run	HV	PreAmp	non-Lin	Error	$\chi^2/6df$
1896	-1150	0.5	0.426	0.075	2.420	1843	-860	0.1	0.904	0.227	16.77
1897	-1120	0.5	0.320	0.123	5.564	1844	-840	0.1	0.869	0.251	25.18
1898	-1080	0.5	0.228	0.093	2.871	1845	-820	0.1	1.269	0.346	26.10
1899	-1040	0.5	0.200	0.120	5.120	1846	-800	0.1	0.848	0.295	29.19
1905	-1110	0.6	0.502	0.172	7.533	1847	-860	0.1	1.355	0.247	15.99
1906	-1080	0.6	0.268	0.125	8.046	1848	-840	0.1	1.054	0.194	14.76
1907	-1050	0.6	0.227	0.186	8.355	1849	-820	0.1	0.492	0.194	17.84
1908	-1020	0.6	0.389	0.083	2.008	1850	-800	0.1	1.211	0.541	98.22
1901	-1010	1.0	0.431	0.102	3.712	1834	-720	0.3	-0.148	0.163	9.668
1902	-980	1.0	0.182	0.193	16.58	1835	-700	0.3	-0.179	0.229	9.338
1903	-950	1.0	0.287	0.091	2.936	1837	-675	0.3	-0.104	0.242	13.89
1904	-920	1.0	0.137	0.112	3.769	1838	-650	0.3	0.205	0.316	24.99
1910	-890	2.0	0.027	0.146	7.582	1830	-650	0.5	-0.190	0.111	2.923
1912	-870	2.0	0.159	0.116	3.802	1831	-630	0.5	0.148	0.348	39.38
1913	-840	2.0	-0.154	0.160	4.930	1832	-610	0.5	-0.268	0.213	9.548
1914	-810	2.0	-0.162	0.151	7.075	1833	-595	0.5	-0.301	0.208	7.082
1919	-770	4.0	0.072	0.210	7.561	1839	-645	0.6	-0.079	0.157	6.576
1916	-750	4.0	-0.019	0.120	4.032	1851	-630	0.6	-0.308	0.084	2.558
1917	-730	4.0	0.133	0.130	3.262	1841	-610	0.6	-0.424	0.134	5.048
1918	-710	4.0	-0.130	0.117	3.480	1842	-590	0.6	0.065	0.383	29.23
1920	-650	10.0	0.139	0.202	8.691	1826	-570	1.0	-0.325	0.190	7.729
1921	-630	10.0	0.071	0.150	4.912	1827	-555	1.0	-0.397	0.228	9.533
1922	-610	10.0	0.256	0.144	2.719	1828	-540	1.0	-0.460	0.221	15.22
1923	-590	10.0	0.223	0.195	6.154	1829	-520	1.0	-0.099	0.170	5.098
1915	-750	4.0	-0.019	0.120	4.032	1819	-500	2.0	-0.428	0.166	5.703
1917	-730	4.0	0.133	0.130	3.262	1820	-490	2.0	-0.518	0.124	3.582
1918	-710	4.0	-0.130	0.117	3.480	1821	-475	2.0	-0.301	0.159	4.882
1920	-650	10.0	0.139	0.202	8.691	1822	-460	2.0	-0.469	0.241	9.740

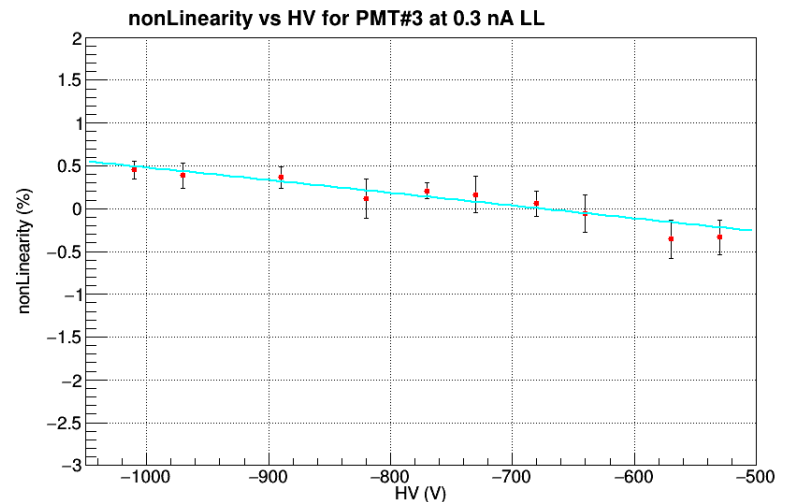
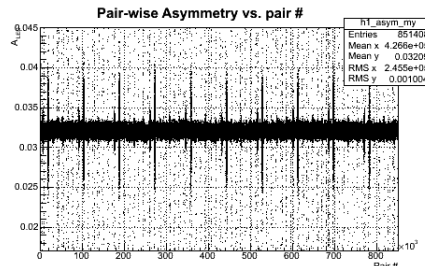
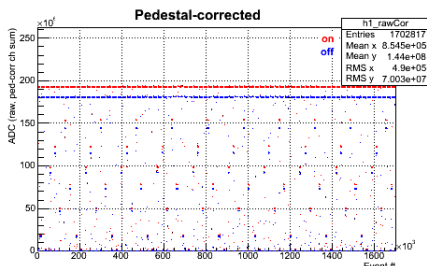
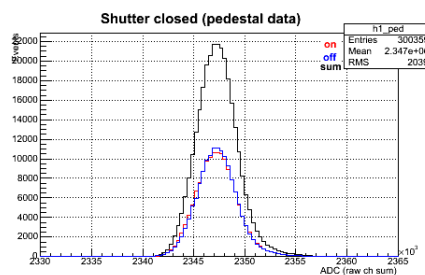
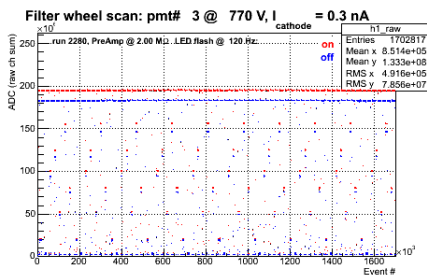
LL = 0.5 nA					
Run	HV	PreAmp	non-Lin	Error	$\chi^2/6df$
1863	-1040	0.5	0.393	0.039	0.7648
1865	-1010	0.5	0.289	0.108	4.324
1866	-980	0.5	0.238	0.051	0.9041
1867	-950	0.5	0.360	0.202	19.54
1857	-1000	0.6	0.393	0.064	1.595
1859	-970	0.6	0.354	0.095	3.488
1860	-940	0.6	0.525	0.212	15.26
1861	-920	0.6	0.297	0.142	5.493
1868	-900	1.0	0.344	0.269	29.49
1869	-880	1.0	0.170	0.184	11.66
1870	-850	1.0	0.331	0.062	0.7265
1872	-830	1.0	0.055	0.231	13.05
1873	-800	2.0	0.206	0.148	5.657
1874	-780	2.0	0.055	0.144	7.464
1875	-760	2.0	0.113	0.114	3.686
1876	-740	2.0	0.469	0.237	16.29
1877	-700	4.0	0.095	0.157	6.243
1878	-680	4.0	0.097	0.114	2.977
1879	-660	4.0	0.053	0.146	4.984
1881	-640	4.0	-0.130	0.166	8.138
1883	-590	10.0	-0.266	0.130	3.332
1884	-570	10.0	0.166	0.124	3.616
1885	-550	10.0	-0.237	0.186	6.346
1886	-530	10.0	-0.009	0.197	5.260

LL = 10.0 nA					
Run	HV	PreAmp	non-Lin	Error	$\chi^2/6df$
1786	-780	0.1	0.038	0.139	9.707
1785	-760	0.1	0.333	0.330	21.84
1782	-740	0.1	-0.163	0.244	18.23
1783	-720	0.1	-0.160	0.187	11.51
1787	-780	0.1	0.262	0.204	22.53
1788	-760	0.1	-0.057	0.092	3.948
1789	-740	0.1	-0.060	0.247	20.74
1790	-720	0.1	-0.417	0.122	7.334
1791	-660	0.3	-0.743	0.171	5.325
1792	-640	0.3	-0.698	0.241	12.76
1793	-620	0.3	-0.672	0.380	23.75
1794	-600	0.3	-0.885	0.325	35.99
1799	-590	0.5	-0.920	0.274	26.76
1800	-570	0.5	-0.901	0.271	16.07
1801	-550	0.5	-1.015	0.320	33.61
1802	-530	0.5	-1.231	0.265	14.08
1795	-575	0.6	-1.042	0.254	10.40
1796	-555	0.6	-1.205	0.164	5.487
1803	-535	0.6	-1.378	0.253	16.20
1798	-520	0.6	-1.446	0.374	21.15
1804	-520	1.0	-0.998	0.411	29.96
1805	-505	1.0	-1.421	0.379	23.99
1806	-490	1.0	-1.506	0.458	25.02
1807	-480	1.0	-1.780	0.528	53.54
1808	-460	2.0	-1.530	0.253	12.60
1809	-450	2.0	-1.865	0.252	16.29
1810	-435	2.0	-1.870	0.376	26.69
1811	-425	2.0	-1.823	0.348	17.32

A Different Approach of Measurement (from Kent)

- Go back to 100 % transmission setting after each filter measurement
- Each filter stays in its position for 20 sec
- 100 % transmission position stays in its position for 60 sec
- Shutter remains close for 8 sec during each filter change
- Filter wheel rotates 10 cycles
- Takes about 2 hrs to collect 1.7 M events

Run	HV	PreAmp	non-Lin	Error	$\chi^2/6df$
2289	-1010.0	0.5	0.454	0.102	1.571
2290	-970.0	0.5	0.387	0.144	8.671
2287	-890.0	1.0	0.364	0.127	1.943
2288	-820.0	1.0	0.018	0.224	4.546
2280	-770.0	2.0	0.210	0.095	3.228
2281	-730.0	2.0	0.165	0.216	3.021
2282	-680.0	4.0	0.060	0.148	4.632
2284	-640.0	4.0	-0.053	0.219	3.967
2285	-570.0	10.0	-0.357	0.223	11.08
2286	-530.0	10.0	-0.335	0.200	8.374



Summary and Future Plans

- So far, results are very promising; we should meet or surpass PMT non-linearity systematic error requirements
- PMT non-linearity shows a linear relation with high voltage
- There is always a certain high voltage above which the non-linearity changes its sign
- Results from constant temperature technique agree with those from our regular measurement technique
- Planning to repeat the measurements
- Still planning to explore the Qweak style non-linearity measurements which use 3 LEDs (two of them flashing at different rates and one steady)

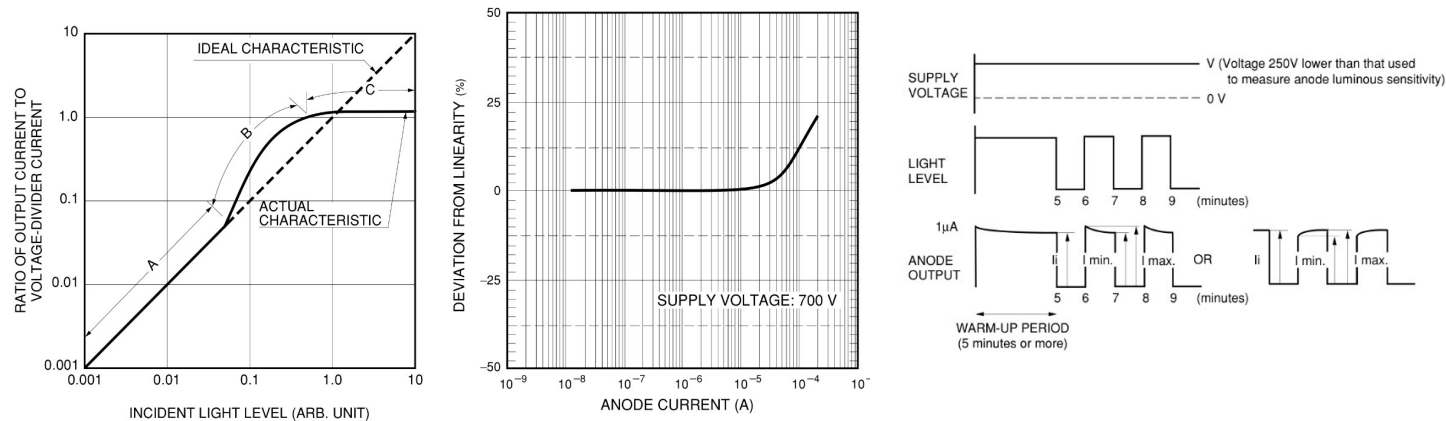
THANK YOU

All the plots of the study can be found at:

daq3.physics.isu.edu/linearity/PMT.html.

Extra Slides

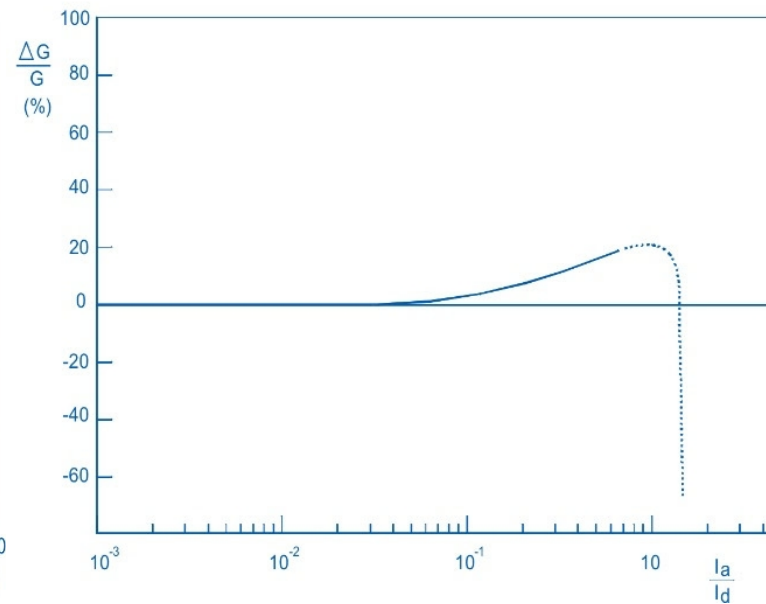
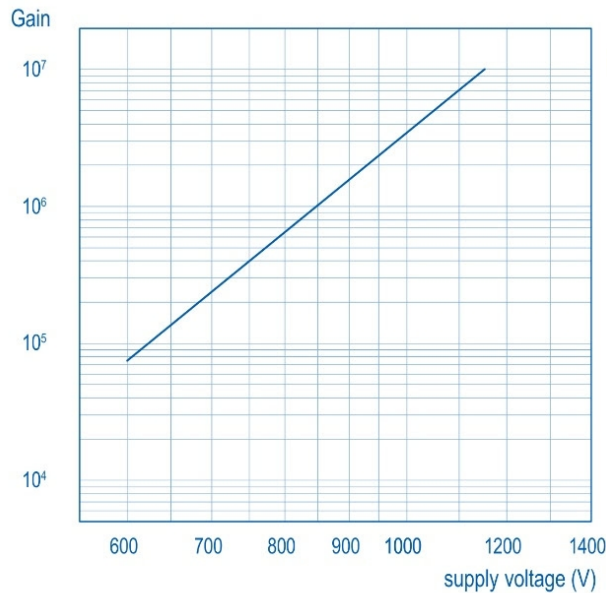
PMT characteristics from Hamamatsu handbook



- At high currents, space charge can influence the electron trajectory, causing collection losses.
- Light level $>$ certain level – PMT output becomes saturated and is no longer proportional to the light level.
- Light hysteresis and voltage hysteresis of the PMT.
- Signal to noise ratio of the PMT.
- Drift (time stability) – warm up helps minimize.
- PMT operation stability depends on the total stability of the power supply characteristics (drift, ripple, temperature, input regulation, load regulation).

hamamatsu.com/resources/pdf/etd/PMT_handbook_v3aE.pdf

PMT characteristics from Photonis



- PMT gain varies as a power of the supply voltage:

$$\frac{G_2}{G_1} = \left(\frac{V_2}{V_1} \right)^{\alpha N}$$

- $\alpha \in [0.6, 0.8]$, N is the number of dynodes.
- Gain varies as a function of I_a/I_d . I_a is the actual anode current and I_d is the divider current.

particle.korea.ac.kr/lab/cata_basic.pdf