## CS 4412 : Algorithm Analysis

## Homework Assignment \#15

Show all work neatly.
Question 1: (5) You are given five matrices with the following dimensions:

- $\mathrm{M}_{1}: 20 \times 5$
- $\mathrm{M}_{2}: 5 \times 10$
- $\mathrm{M}_{3}: 10 \times 12$
- $\mathrm{M}_{4}: 12 \times 6$
- $M_{5}: 6 \times 25$

You wish to compute the product of the matrix chain $M_{1} M_{2} M_{3} M_{4} M_{5}$. What is the optimal (minimal) number of scalar multiplications required to compute this product? Use dynamic programming to compute the answer and show your work.

Question 2: (5) For the following graph, step through Floyd's algorithm (Floyd-Warshall), showing the $\mathbf{D}$ matrix at each step, and report the resulting shortest paths between all pairs of vertices.


